


BEST PRACTICE AS ACTUAL AND RELATIVE BENCHMARK TO INEFFICIENT UNITS: MULTISSET DEA ANALYSIS

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Summary:

The direction in research of the efficiency of decision-making units in this paper is an efficient→multi-inefficient→multi-efficient unit. So, the general purpose of this paper is twofold: (1) identification of «hidden» inefficient units within a multi-set, among efficient units of the basic set, and (2) achieving the efficiency in such identified inefficient units. This indicates (warns of!) a negative efficient→inefficient process, so as to provide a timely response and thereby prevent multi-inefficiency. The specific goal is to assess the efficiency of the Serbian railway passenger stations, first within the basic set of the Passenger Transport Section Belgrade, then in the multi-set of the Passenger Transport Sections, and finally in the superset, the Passenger Transport Sector. This is achieved by means of the multi-set DEA (Data Envelopment Analysis) method, which is a system for: (i) relative efficiency assessment, in the first iteration, through the basic set analysis, and (ii) decrease in efficiency of potentially inefficient units, in subsequent iterations, through the multi-set analysis. The result is that the efficient stations Požarevac and Pančevo Bridge are at the initial level, and the (newly) efficient Požarevac, Novi Sad and Inđija at the final level. The best practice station remains the Požarevac Station, which is multi-efficient, and therefore the role model to inefficient stations. The conclusion is drawn that the solution resulting from the multi-set DEA analysis is more realistic, and less relative, because it applies to a wider analysed set of decision-making units, i.e., a larger coverage when considering the issue. This is important for fitting into the new era of growing globalization, and therefore our recommendation is the integral multi-set, as opposed to the individual single set approach.

Key words: Efficiency, Data Envelopment Analysis, Multi-Set Analysis, Railway Stations.

Introduction

A number of same-type organisational units within a single organisation jointly accomplish the objective of the organisation, thereby contributing to a higher or lesser extent. In order for the organisation to be successful, it is necessary for all of its units to be successful. Success is a multidimensional concept, with efficiency being one of its dimensions.

Efficiency is a feature of someone or somebody (people, institutions, organisations, companies, processes and other) to produce maximum output (products, services) using minimum input (resources, activities). Expressed in the simplest mathematical terms, it is the ratio of an output and an input. From a more complex mathematical point of view, it is a ratio between the weighted sum of multiple outputs and weighted sum of multiple inputs. For this purpose, the *Data Envelopment Analysis*, (DEA) was created in 1978 by *Charnes, Cooper and Rhodes* as a method of calculating the efficiency of the so-called *Decision Making Units*, abbreviated DMU), (Charnes et al, 1978).

The idea of this paper is to decrease the relativity and to increase the reality of the best practice through the iterative procedure "efficient→inefficient" (efficient unit in the basic set, inefficient in the multiset). Thus, success is a relative and changeable category and requires caution and constant reconsideration. With the view to the future, the goal of this paper is an early discovery of potentially inefficient so-called "hidden" units, and their respective timely redirecting.

Among numerous examples of best practices of similar companies, both local and foreign, the most suitable example is a so-called personal example, and that is the example of the same analysed set of measuring units. This is because all the units of the same company as means of their teamwork, under the same conditions, contribute to the accomplishment of a single goal. Logical conclusion is the requirement for all the units to proportionally contribute to this objective, whereby inefficient units imitate the efficient ones. And when those efficient units, acting as models for the inefficient ones, are "among us" or "ours", we believe that the efficiency can really be achieved.

On the one hand, the Sensitivity analysis of a single same set of decision making units, but applying different input/output data and opposite DEA models, results in the same efficiency (Vuković, 2016). On the other hand, the stated Multiset DEA analysis of the same data of decision-making units in a number of different, ever bigger sets, results in smaller or equal efficiency, so some efficient units become inefficient. By

application of the post DEA sensitivity analysis, newly efficient units become efficient in a wider set, a so-called multiset. Thus the research direction is efficient→multiinefficient→multiefficient units. From this point of view, the goal is two steps ahead: recognition of potentially inefficient units and achieving efficiency in a wider set. Multiset efficiency is more weighted than the monoset, as is it obtained by further decrease of input and/or increase of output, thereby improving the operation of units, which defines the contribution of our paper.

The following chapters include the overview of references, the short descriptions of the DEA method and the Multiset DEA analysis, as well as a numerical example, while the conclusion has been provided based on the stated information.

Overview of references

Having reviewed the newly published worldwide and local literature, we herewith provide the following observations:

1. Efficiency is monoset-oriented, where each decision-making unit is analysed in the same set. Examples of such sets include: 208 clinical commissions in England (Takundwa et al, 2017), 42 bus routes in Brisbane, Australia (Tran et al, 2017), and 55 universities in the state of Mexico (Sagarra et al, 2017). While in these works each unit is analysed in the same set, we here observe a unit in a wider scale, as an element of every bigger set. It is thus possible to compare the efficiency results obtained through multisets and to provide a more realistic assessment of efficiency.

2. The problem of the multiset prediction is not well known in the literature. According to certain authors, the problem is solved by consecutive decision-making, where a new multiset function of loss is proposed as a parameter of predictive policy (Welleck et al, 2017). According to others, the multiset approach is used to predict the average daily temperature, as shown by the Taipei example in Taiwan (Vamitha & Rajaram, 2015). In our paper, the Multiset DEA analysis of units is used for predicting inefficient results, which meant increasing the set of decision-making units by adding a new set. In this way, potentially inefficient units are more accurately predicted, which is helpful in solving the problems of multiset prediction.

3. The multiset theory differentiates between conventional and fuzzy logic. Conventional logic defines whether an element belongs to a set by "yes or no", whereas fuzzy logic does so by "more or less" (Pamučar et al, 2016). The Multiset DEA analysis is a connection between the

multiset theory and the DEA method. The stated analysis defines the simultaneous belonging of elements to a larger number of sets by "yes", with multiset efficient units. In addition, it also uses "yes", with multiset inefficient units. Realistically, a multiset is a family of a set of efficient and a set of inefficient units. Units "more or less" belong to a multiset, where units closer by efficiency belong to a multiset "more", and with the deviation "less".

4. Efficiency is dealt with without burdening the external society, but individually instead, within the scope of internal potential. The example of this case are premises used by institutions, command departments and units of the Serbian Army, where the application of thermal isolation is proposed to solve the problem of energy efficiency (Živković & Banjac, 2016). By applying the stated idea of using internal potential, we are solving a complex problem of efficiency of railway stations, with an additional idea of using its diverse potential, not just material but also organisational, and thereby achieving certain savings.

5. Organisational efficiency is impossible without the evaluation of the work of employees, which requires management so that it could be managed (maximised) in this way (Lukovac et al, 2014). Measurement of work at different levels by a multiset approach is a higher stage of comparison.

Core principles of DEA (Data Envelopment Analysis)

DEA is a method of mathematical programming for the calculation of efficiency and it is used, from a wider perspective, in economy, and more precisely, in different kinds of economics, depending on the type of decision making units. This is supported by numerous and diverse examples from the world and local literature, covering different types of Economics:

– Health Economics, where the effectiveness of health organizations is being decided upon (an example of this type of units is the public health system and the medical protection system of the OECD countries (Ozcan & Khushalani, 2017);

– Traffic Economics, where the effectiveness of transport organizations is being decided upon (examples are the Brazilian intermodal terminals), (Peixoto et al, 2017);

– Sports Economics, where the decision on the efficiency of sports organizations is being decided upon (for example, the football team of Serbia), (Petrović Đorđević, 2015);

- Tourism Economics, involving decision making on the efficiency of tourism organizations (e.g. ecotourism parks), (Lin et al, 2017);
- Business Economics, where the effectiveness of business organizations is being decided upon (for example, Taiwanese insurance companies), (Chen & Zhu, 2017);
- Economics of Education, where the decision making on the effectiveness of educational organizations is being decided upon (examples are Chinese educational organizations, from pre-school to higher education), (Si & Qiao, 2017);

The algorithm of the selection process with the DEA method application includes five steps, as presented in Figure 1.

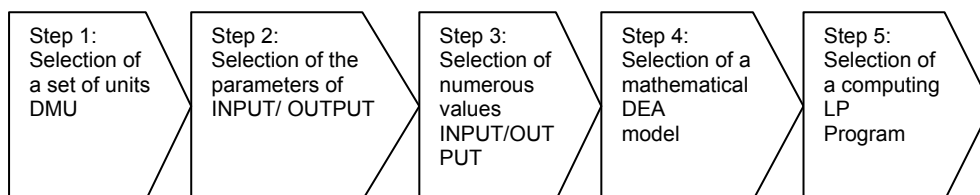


Figure1 – DEA method application algorithm
Рисунок 1 – Алгоритм применения АОД метода
Слика 1 – Алгоритам примене ДЕА методе

According to Figure 1, each example of a particular DEA method is characterised by the concrete: decision making units (DMU), input-output parameters (INPT/OUPT), numerous values of input and output, mathematical DEA model (Charnes et al, 1978), (Banker et al, 1984), (Yang et al, 2000), and a computer program (MS Excel Solver, LINDO, LINGO and other) for solving linear programming (LP) tasks, whose result is the efficiency value for each decision making unit.

By the application of the DEA method, decision making units are divided into two groups: efficient ($Eff=1$) and inefficient ($0 < Eff < 1$), while according to their numerical values they have a number of comparison stages, so it is possible to establish a ranking (complete or incomplete) of decision making units. Efficient units obtained based on the actual data are realistically best practice units, but they are also a substandard of efficiency as they are valid only for a concrete example (case study). Opposite to this is a generally applied standard which does not exist in this case, as there is no absolute efficiency.

Multiset DEA analysis

The Multiset DEA analysis is based on the fact that sets are not of exact size, but can be changed depending on the number of elements. Hence, the limit i.e. the final size of a set remains unknown. And it is exactly the issue of the limit of the set, being the analysis framework, which is significant for the efficiency value. The above analysis contains the principle that all the units outside the basic set break the ranking of the units of the basic set, by the value of efficiency, by analysing them in sets, which are at different (organizational, hierarchical) levels. A complete set is not known, so it is unknown which is the highest possible efficiency i.e. only experiential efficiency is known.

Similar to Savić's idea (Savić, 2017) that the algorithm should be applied several times, whereby a single input or output is added in each iteration, the idea of our paper is to add more decision-making units to each iteration, i.e. a new set of DMUs which represent a single organizational unit. However, while in the previously stated reference "turning" points among the iterations referred to the inputs/outputs (qualitative characteristics of the DMU), the "turning" points here are the sets of DMUs (quantitative characteristics). Changing qualitative features or changes of content are a feature of a systemic approach, while the change in quantitative characteristics or changes in the size of a set of features, discussed herewith, is a multi-set approach.

The multiset DEA analysis estimates the efficiency of the decision-making unit, where a unit is an element in each iteration of a new wider set. The first DEA model which we will use, from which many modified models are devised, is the CCR model (Charnes et al, 1978) whose multiset mathematical formulation consists of sets of decision making units in which the goal function is maximized with the set limits, Table 1.

According to Table 1, the Multiset DEA analysis is an iterative process of maximizing the function of the objective h_o (efficiency) under the given restrictions, in ever increasing set till the final total sum set of all p basic sets (BSp).

The idea of the Multiset analysis is contrary to the idea of the post DEA Sensitivity Analysis. The Sensitivity analysis yields targeted activities (target values of inputs and outputs), which by the realization of an inefficient unit become effective. Contrary to this, the Multiset analysis is a kind of prediction that produces non-targeted (undesirable) inefficient units, by making some efficient units inefficient in the multiset, Figure 2.

Table 1 – Multi-Set DEA Analysis Mathematical Model
 Таблица 1 – Математическая модель Мульти-множественного АОД анализа
 Табела 1 – Математички модел мултискуповне ДЕА анализе

Multi-set model	DEA model	Meaning of symbols
$DMU_j \in \{OS_1\} \cup \{OS_2\} \cup \dots \cup \{OS_p\}$ $\{OS_1\} \cup \{OS_2\} \cup \dots \cup \{OS_p\} = \{NS\}$ $OS_1 = \{DMU_1, DMU_2, \dots, DMU_a\}$ $OS_2 = \{DMU_{a+1}, \dots, DMU_b\}$... $OS_p = \{DMU_{d+1}, \dots, DMU_g\}$	$\max h_0 = \frac{\sum_{r=1}^s u_r y_{r0}}{\sum_{i=1}^m v_i x_{i0}}$ $\frac{\sum_{r=1}^s u_r y_{rj}}{\sum_{i=1}^m v_i x_{ij}} \leq 1$ $j = 1, \dots, n$ $u_r \geq 0, r = 1, \dots, s$ $v_i \geq 0, i = 1, \dots, m$	h_0 – efficiency of DMU for which is calculated y_{rj} – output of j DMU x_{ij} – input of j DMU n – number of DMU m – number of input s – number of output u_r – weighted coefficient of r output v_i – weighted coefficient of i input p – no. of OS $a, b, c, \dots, d, \dots, g$ – no. of elements of BS

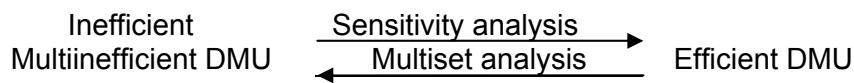


Figure 2 – Two-way process of efficiency change
 Рисунок 2 – Двухнаправленный процесс изменения эффективности
 Слика 2 – Двосмерни процес промене ефикасности

According to Ljubisav Rakić: "The position of science in the century which has begun is to change the methodology. Instead of studying why something happened, we should move in the direction of predicting and studying of what could happen." (Rakić, 2017)

The essence of the Sensitivity analysis is as follows: (1) improving the efficiency of decision making units, and (2) aiming at proportionally equal contribution of all units of a set to the common goal of the company. The essence of opposite, multiset approach is viewing the units in a wider context.

The philosophy of the multiset approach may be explained by a modern theory included in the quotation of Stuart Diamond: "Each ceiling is a new floor", expressed in such a way to say that we could always get more (but not everything), which is also the name of his book (Diamond, 2015, p.36). Applied to the topic of our paper, provided efficiency is the

ability to maximise the results with the least possible investment - it means that by widening the analysed set by inclusion of new units we can get the efficiency of higher weight (the efficiency of the units of the basic set decreases or remains the same with multiset efficient units).

Within the context of the multiset DEA analysis of efficiency, this means that the current efficiency is disturbed by inclusion of new units and may always be overcome by new units included in the set of the analysed units, and thus new efficient units are being formed.

If, according to Marjanović (Vešović et al, 2007), the basic goals of the company are survival, facilitation of survival (efficiency of operation) and progress, then within the context of the multiset approach:

1. The current state of the set indicates: the survival (the organisation is operating with both efficient and inefficient units).

2. Targeted state of the set obtained by the Sensitivity analysis marks: Facilitating survival (as a result of targeted activities, all inefficient units become efficient).

3. Higher targeted state of the set obtained by Multiset DEA analysis marks: Progress (as the result of increase in the size of the set, the criterion for reaching efficiency has become more demanding, as the former efficient units with the same values of input-output parameters become inefficient). Therefore, the efficiency in a larger set is more weighted than the efficiency in smaller set.

Real evaluation of the efficiency for the previous period is performed by solving the preferred DEA model, or Ex-post evaluation of efficiency (backwards evaluation) for each of the analysed units of decision making. The sensitivity analysis provides the desired estimation for the future period or Ex-ante evaluation of efficiency (forward evaluation), only for inefficient units of decision making (efficient decision making units already have the desired efficiency for the unit).

Case study: Railway stations of IŽS Company

The Multiset DEA analysis is a universal system for the evaluation of efficiency of entities and their arrangement according to a given efficiency, within diverse numeric examples. However, with each individual application, it is necessary for entities to be of the same kind, as it is widely known and logical that comparison makes sense only in such circumstances. A realistic example of such entities are Serbian railway passenger stations, which are subject of our research with the aim of illustrating the stated analysis. But, why railway, why railway stations and why at this moment?

Railway is a type of transport for passengers and goods, used for civil purposes, for transporting people and equipment, and also for military purposes. Theoretically, its advantages are numerous and important in terms of transport power, traffic safety, spatial acquisition, consumption of energy, emissions of harmful substances, noise and other, which make it competitive. Railway stations are important infrastructure facilities in the transport process; apart from this, they are numerous, and financially valuable. They are also important to us as a place of departures and arrivals, loadings and unloadings. In the new era of business, according to the principle of a liberal, supranational market, it is compulsory for companies to be efficient and trending for continuous improvement. Hence, it is necessary to continuously monitor and comply with complex and expensive interoperability flows. To this purpose, a case study: Serbian Railway Passenger Stations.

On the one hand (theoretically), Serbian railway passenger stations are decision making units (DMU) within the DEA method, and on the other hand (practically), railway stations (RS) are infrastructural facilities within the *Infrastruktura železnica Srbije* Company (IŽS), Table 2. Six-set DEA analysis following the enlargement of a single-set example (Vuković, 2016).

Table 2 – Example in practice of the Serbian railways
Таблица 2 – Пример из практики сербских железных дорог
Табела 2 – Пример из праксе српских железница

DEA method			IŽS company		
DMU as element of DEA			RS as element of IŽS		
Superset	Set	Subset	Railway station	Section	Sector
LS 73 DMU	BS1 16 DMU	DMU1	Belgrade	1.Passanger Transport Section Belgrade (including OU Pančevo and OU Požarevac)	Passenger Transport Sector
		DMU2	Mladenovac		
		DMU3	Rakovica		
		DMU4	Zemun		
		DMU5	Batajnica		
		DMU6	Novi Belgrade		
		DMU7	Pančevo Bridge		
		DMU8	Resnik		
		DMU9	Pančevo Main		
		DMU10	Vršac		
		DMU11	Pančevo Town		

DEA method			IŽS company		
DMU as element of DEA			RS as element of IŽS		
Superset	Set	Subset	Railway station	Section	Sector
		DMU12	Požarevac		
		DMU13	Smederevo		
		DMU14	Mala Krsna		
		DMU15	Vranovo		
		DMU16	Radinac		
	BS2 12 DMU	DMU17	Lapovo	2. Passanger Transport Section Lapovo (including OU Kraljevo)	
		DMU18	Jagodina		
		DMU19	Stalać		
		DMU20	Paraćin		
		DMU21	Velika Plana		
		DMU22	Ćuprija		
		DMU23	Ćičevac		
		DMU24	Palanka		
		DMU25	Kraljevo		
		DMU26	Kragujevac		
		DMU27	Raška		
		DMU28	Čačak		
	BS3 12 DMU	DMU29	Niš	3. Passenger Transport Section Niš (with OU Zaječar)	
		DMU30	Leskovac		
		DMU31	Pirot		
		DMU32	Dimitrovgrad		
		DMU33	Vranje		
		DMU34	Palilulska Rampa		
		DMU35	Crveni Krst		
		DMU36	Aleksinac		
		DMU37	Zaječar		
		DMU38	Knjaževac		
		DMU39	Negotin		
		DMU40	Bor		
	BS4 18 DMU	DMU41	Novi Sad	4. Passenger Transport Section Novi Sad (including OU Ruma and OU Zrenjanin)	
		DMU42	Beška		
		DMU43	Čortanovci		
		DMU44	Sremski Karlovci		
		DMU45	Vrbas		
		DMU46	Odžaci		
		DMU47	Zmajev		
		DMU48	Petrovaradin		

DEA method			IŽS company		
DMU as element of DEA			RS as element of IŽS		
Superset	Set	Subset	Railway station	Section	Sector
		DMU49	Ruma		
		DMU50	Šabac		
		DMU51	Šid		
		DMU52	Indija		
		DMU53	Stara Pazova		
		DMU54	Nova Pazova		
		DMU55	Sremska Mitrovica		
		DMU56	Zrenjanin		
		DMU57	Zrenjanin Factory		
		DMU58	Kikinda		
	BS5 8 DMU	DMU59	Subotica	5. Passenger Transport Section Subotica	
		DMU60	Sombor		
		DMU61	Sonta		
		DMU62	Prigrevica		
		DMU63	Senta		
		DMU64	Bogojevo		
		DMU65	Žednik		
		DMU66	Horgoš		
	BS6 7 DMU	DMU67	Užice	6. Passenger Transport Section Užice	
		DMU68	Požega		
		DMU69	Priboj		
		DMU70	Valjevo		
		DMU71	Prijepolje		
DMU72		Lazarevac			
DMU73		Lajkovac			

Based on Table 2, there are 73 railroad stations within the network of Serbian Railways. They are organized in two levels: (1) Passenger Transport Sector, at a higher organizational level; and (2) Passenger Transport Section, at a lower organizational level. The sector includes six sections, four of which have organizational units (OU), as a lower organizational level. The seats of the Sections (Belgrade, Lapovo, Niš, Novi Sad and Subotica) are important railway hubs, where more lines are obtained, with more intensive traffic volumes, and are commercially significant places. By the very nature of their operation, the mutual cooperation of the Sections is very important because they are connected: (1) physically, by railroad tracks; (2) organizationally, by

traffic connections (both railways and connections are usually administered by two or more Sections). Hence, it is important that they are all efficient, in order to maintain the continuity of the technological process of work. Namely, the inefficiency of one of them jeopardizes the efficiency of any other.

If we select the following input/output parameters as follows:

- The man: "basic factor of each production, including the production of transport or post office service. It simultaneously appears as its organiser, manager and executor." (Vešović et al, 2007. p.186),

- Produced service: "Standard measure of the volume of the whole economy is the gross domestic product (GDP), which represents the value of all goods and services produced in an economy within a year." (Stiglitz, 2008, p.38),

- Work performance: the purpose, and therefore the point of performing the works, is to gain profit,

then the following parameters are selected in our case according to the given logic: (i) number of cashiers (entry 1), (ii) number of dispatched trains (entry 2), (iii) number of dispatched passengers (exit). The sources of the concrete data for our case include:

- Job classification within the company in 2010: number of cashiers, (Železnice Srbije, 2010);

- Timetable 2013/2014: number of trains, (Železnice Srbije, 2013);

- Statistics of Serbian Railways 2013: number of passengers, (Železnice Srbije, 2014).

The option A of the multi-set DEA analysis analyses units in each basic set individually (left side of Table 3) and units in the total sum superset (right side of Table 3). The application of the CCR DEA model from Table 1 results in the values of efficiency of decision making units evaluated by *MS Excel Solver* to six decimal numbers, Table 3.

According to Table 3, the application of the Section analysis resulted in the total of 12 efficient units, which are the best practice units, whereas the Sector analysis resulted in only three efficient units: Požarevac, Novi Sad and Indjija. The remaining nine, DMU7,18,24,25,30,37,59,66 and 67, so called "hidden" inefficient units, have been discovered by the analysis of the superset of Sectors, where they become inefficient.

This indicates the sensitivity of the DEA method to a change in a set size. A quotation of Andersen and Petersen states (Andersen & Petersen, 1993, p.1261): *A weakness of DEA is that a considerable number of observations typically is characterized as efficient, unless the sum of the number of inputs and outputs is small relative to the number of observations.*

Table 3 – Decision-making unit efficiency in the basic sets and in a superset
Таблица 3 – Эффективность единиц принятия решений в основном множестве и надмножестве

Табела 3 – Ефикасност јединица одлучивања у основним скуповима и надскупу

VARIANT A							
No of BS.	DMU no.	Efficiency (0–1]	Quantity of efficient units	SS	DMU no.	Efficiency (0–1]	Quantity of efficient units
Basic set 1	DMU1	0.879175	2	Superset	DMU1	0.798903	3
	DMU2	0.192230			DMU2	0.170841	
	DMU3	0.206022			DMU3	0.175874	
	DMU4	0.164341			DMU4	0.140289	
	DMU5	0.361602			DMU5	0.308687	
	DMU6	0.181727			DMU6	0.155137	
	DMU7	1.000000			DMU7	0.961284	
	DMU8	0.093544			DMU8	0.079853	
	DMU9	0.359357			DMU9	0.341007	
	DMU10	0.862869			DMU10	0.765826	
	DMU11	0.323213			DMU11	0.298594	
	DMU12	1.000000			DMU12	1.000000	
	DMU13	0.603945			DMU13	0.533680	
	DMU14	0.302814			DMU14	0.258497	
	DMU15	0.100037			DMU15	0.087856	
	DMU16	0.139338			DMU16	0.122371	
Basic set 2	DMU17	0.113290	3		DMU17	0.039702	
	DMU18	1.000000			DMU18	0.350449	
	DMU19	0.248430			DMU19	0.075714	
	DMU20	0.757351			DMU20	0.164219	
	DMU21	0.589529			DMU21	0.148776	
	DMU22	0.312563			DMU22	0.100666	
	DMU23	0.267623			DMU23	0.083624	
	DMU24	1.000000			DMU24	0.345956	
	DMU25	1.000000			DMU25	0.256134	
	DMU26	0.633900			DMU26	0.137451	
	DMU27	0.466613			DMU27	0.123317	
	DMU28	0.913229			DMU28	0.304692	
Basic set 3	DMU29	0.982846	2		DMU29	0.674760	
	DMU30	1.000000			DMU30	0.660572	
	DMU31	0.306841			DMU31	0.204181	
	DMU32	0.259709			DMU32	0.172817	

Vuković, D., Best practice as actual and relative benchmark to inefficient units: multiset DEA analysis, pp.525-550

VARIANT A							
No of BS.	DMU no.	Efficiency (0–1]	Quantity of efficient units	SS	DMU no.	Efficiency (0–1]	Quantity of efficient units
Basic set 3	DMU33	0.439482			DMU33	0.148063	
	DMU34	0.249361			DMU34	0.165932	
	DMU35	0.555812			DMU35	0.187271	
	DMU36	0.647396			DMU36	0.367192	
	DMU37	1.000000			DMU37	0.877614	
	DMU38	0.490002			DMU38	0.320747	
	DMU39	0.472408			DMU39	0.303723	
	DMU40	0.767057			DMU40	0.468147	
Basic set 4	DMU41	1.000000	2		DMU41	1.000000	
	DMU42	0.488504			DMU42	0.488504	
	DMU43	0.266385			DMU43	0.266385	
	DMU44	0.148627			DMU44	0.148627	
	DMU45	0.544243			DMU45	0.544243	
	DMU46	0.126275			DMU46	0.126275	
	DMU47	0.307956			DMU47	0.307956	
	DMU48	0.133064			DMU48	0.133064	
	DMU49	0.215982			DMU49	0.215982	
	DMU50	0.327164			DMU50	0.327164	
	DMU51	0.340419			DMU51	0.340419	
	DMU52	1.000000			DMU52	1.000000	
	DMU53	0.732659			DMU53	0.732659	
	DMU54	0.522205			DMU54	0.522205	
	DMU55	0.422567			DMU55	0.422567	
	DMU56	0.387019			DMU56	0.387019	
DMU57	0.022979	DMU57	0.022979				
DMU58	0.041560	DMU58	0.041560				
Basic set 5	DMU59	1.000000	2		DMU59	0.477291	
	DMU60	0.721202			DMU60	0.321932	
	DMU61	0.558896			DMU61	0.178442	
	DMU62	0.584930			DMU62	0.186759	
	DMU63	0.166865			DMU63	0.074945	
	DMU64	0.063039			DMU64	0.020127	
	DMU65	0.873175			DMU65	0.278792	
	DMU66	1.000000			DMU66	0.443437	

VARIANT A							
No of BS.	DMU no.	Efficiency (0–1]	Quantity of efficient units	SS	DMU no.	Efficiency (0–1]	Quantity of efficient units
Basic set 6	DMU67	1.000000	1		DMU67	0.774963	
	DMU68	0.602181			DMU68	0.296396	
	DMU69	0.691438			DMU69	0.470662	
	DMU70	0.955143			DMU70	0.508139	
	DMU71	0.661295			DMU71	0.419728	
	DMU72	0.521605			DMU72	0.191992	
	DMU73	0.135552			DMU73	0.049899	
Totally efficient units			12	Totally efficient units			3

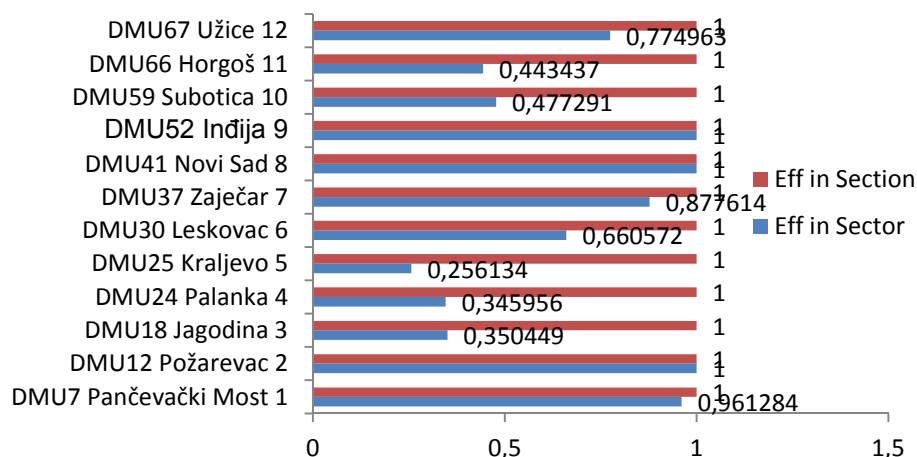


Figure 3 – Best practice units in the Section (12 units) and the Sector (3 units)
 Рисунок 3 – Единицы передовой практики в Секции (12 единиц) и Секторе (3 единицы)

Слика 3 – Јединице најбоље праксе у секцији (12 јединица) и сектору (3 јединице)

The ratio between the Sector efficiency ($Eff \leq 1$) and the Section efficiency ($Eff = 1$), for 12 efficient units in the Section, may be seen from the graph presented in Figure 3. The highest span is of DMU25 which is on the verge of efficiency (0.256134/1), with the achieved 25.6% of the goal. The lowest span is with the DMU7, which is firmly efficient (0.961284/1), with the achieved 96.1% of the target.

For the variant B of the multiset DEA analysis, through the iterative procedure, the number of DMUs gradually increases by adding the units of the following basic unit to Basic set 1, up to the superset size, Table 4.

Table 4 – Efficiency of decision-making units in BS1 and aggregate sets
Таблица 4 – Эффективность единиц принятия решения в ОМ1 и суммарных множествах

Табела 4 – Ефикасност јединица одлучивања у ОС1 и збирним скуповима

VARIANT B						
DMU no.	Efficiency					
	1 st iteration (16DMU)	2 nd iteration (28DMU)	3 rd iteration (40DMU)	4 th iteration (58DMU)	5 th iteration (66DMU)	6 th iteration (73DMU)
DMU1	0.879175	0.879175	0.879175	0.798903	0.798903	0.798903
DMU2	0.192229	0.192229	0.192229	0.170841	0.170841	0.170841
DMU3	0.206021	0.206021	0.206021	0.175874	0.175874	0.175874
DMU4	0.164340	0.164340	0.164340	0.140289	0.140289	0.140289
DMU5	0.361602	0.361602	0.361602	0.308687	0.308687	0.308687
DMU6	0.181726	0.181726	0.181726	0.155137	0.155137	0.155137
DMU7	1.000000	1.000000	1.000000	0.961284	0.961284	0.961284
DMU8	0.093543	0.093543	0.093543	0.079853	0.079853	0.079853
DMU9	0.359357	0.359357	0.359357	0.341007	0.341007	0.341007
DMU10	0.862869	0.862869	0.862869	0.765826	0.765826	0.765826
DMU11	0.323213	0.323213	0.323213	0.298594	0.298594	0.298594
DMU12	1.000000	1.000000	1.000000	1.000000	1.000000	1.000000
DMU13	0.603944	0.603944	0.603944	0.533680	0.533680	0.533680
DMU14	0.302814	0.302814	0.302814	0.258497	0.258497	0.258497
DMU15	0.100036	0.100036	0.100036	0.087856	0.087856	0.087856
DMU16	0.139337	0.139337	0.139337	0.122371	0.122371	0.122371
DMU17		0.044929	0.044929	0.039702	0.039702	0.039702
DMU18		0.396589	0.396589	0.350449	0.350449	0.350449
DMU19		0.088672	0.088672	0.075714	0.075714	0.075714
DMU20		0.177537	0.177537	0.164219	0.164219	0.164219
DMU21		0.157789	0.157789	0.148776	0.148776	0.148776
DMU22		0.111534	0.111534	0.100666	0.100666	0.100666
DMU23		0.092086	0.092086	0.083624	0.083624	0.083624
DMU24		0.389268	0.389268	0.345956	0.345956	0.345956
DMU25		0.287488	0.287488	0.256134	0.256134	0.256134
DMU26		0.148598	0.148598	0.137451	0.137451	0.137451
DMU27		0.143906	0.143906	0.123317	0.123317	0.123317
DMU28		0.349139	0.349139	0.304692	0.304692	0.304692

VARIANT B						
DMU no.	Efficiency					
	1 st iteration (16DMU)	2 nd iteration (28DMU)	3 rd iteration (40DMU)	4 th iteration (58DMU)	5 th iteration (66DMU)	6 th iteration (73DMU)
DMU29			0.809804	0,674760	0,674760	0,674760
DMU30			0.762116	0,660572	0,660572	0,660572
DMU31			0.237283	0,204181	0,204181	0,204181
DMU32			0.200835	0,172817	0,172817	0,172817
DMU33			0.173450	0,148063	0,148063	0,148063
DMU34			0.192833	0,165932	0,165932	0,165932
DMU35			0.219377	0,187271	0,187271	0,187271
DMU36			0.408825	0,367192	0,367192	0,367192
DMU37			0.922098	0,877614	0,877614	0,877614
DMU38			0.369195	0,320747	0,320747	0,320747
DMU39			0.348028	0.303723	0.303723	0.303723
DMU40			0.529783	0.468147	0.468147	0.468147
DMU41				1.000000	1.000000	1.000000
DMU42				0.488504	0.488504	0.488504
DMU43				0.266385	0.266385	0.266385
DMU44				0.148627	0.148627	0.148627
DMU45				0.544243	0.544243	0.544243
DMU46				0.126275	0.126275	0.126275
DMU47				0.307956	0.307956	0.307956
DMU48				0.133064	0.133064	0.133064
DMU49				0.215982	0.215982	0.215982
DMU50				0.327164	0.327164	0.327164
DMU51				0.340419	0.340419	0.340419
DMU52				1.000000	1.000000	1.000000
DMU53				0.732659	0.732659	0.732659
DMU54				0.522205	0.522205	0.522205
DMU55				0.422567	0.422567	0.422567
DMU56				0.387019	0.387019	0.387019
DMU57				0.022979	0.022979	0.022979
DMU58				0.041560	0.041560	0.041560
DMU59					0.477291	0.477291
DMU60					0.321932	0.321932
DMU61					0.178442	0.178442
DMU62					0.186759	0.186759
DMU63					0.074945	0.074945
DMU64					0.020127	0.020127

Vuković, D., Best practice as actual and relative benchmark to inefficient units: multiset DEA analysis, pp.525-550

VARIANT B						
DMU no.	Efficiency					
	1 st iteration (16DMU)	2 nd iteration (28DMU)	3 rd iteration (40DMU)	4 th iteration (58DMU)	5 th iteration (66DMU)	6 th iteration (73DMU)
DMU65					0.278792	0.278792
DMU66					0.443437	0.443437
DMU67						0.774963
DMU68						0.296396
DMU69						0.470662
DMU70						0.508139
DMU71						0.419728
DMU72						0.191992
DMU73						0.049899

According to Table 4, in the 1st, 2nd and 3rd iteration the units DMU7 and 12 are efficient. The fourth iteration is "decisive", as in further 4th, 5th and 6th iterations, the efficient units include DMU12, 41 and 52.

The comparative results of the research of the Variants A and B of the Multiset DEA analysis indicate the units which should be further improved (highlighted), and the unit which remains efficient (bold), Table 5. This further indicates the relativity of efficiency, as practices are best, some in supersets, some however in basic sets.

Considering the efficient units from the monoset viewpoint, set BS1 should be partially improved, i.e. just one efficient unit (DMU7), sets BS2, BS3, BS5 and BS6 should completely improve their efficient units, while set BS4 "strong" is a set with both multi-efficient units.

Unit DMU7 is multi-inefficient due to the fact that it has been discovered as potentially inefficient within the multiset of fourth iteration and further to the superset. Based on this, target activities resulting from the Sensitivity analysis are proposed based on decreasing the input and/or increasing the output. Opposite to this, DMU12 unit is a multiset efficient unit, as it still remains as efficient as in the first set after the increase of the analysed set.

As the Passenger Transport Sector does not include the decision making units by which the analysed set would be enlarged, it is possible to add hypothetical units with hypothetical data in future observations and thus establish the complete ranking. In such future iterations, with new hypothetical units, it is necessary to further decrease the investment and/or increase the result for achieving efficiency.

Table 5 – Result of the Multiset DEA analysis (Variant A, Variant B)
 Таблица 5 – Результат мульти-множественного АОД анализа (Вариант А, Вариант Б)
 Табела 5 – Резултат мултискуповне ДЕА анализе (варијанта А, варијанта Б)

Variant A		Variant B			
Basic set	Efficient	Basic set and aggregate basic sets	Efficient	Multi-efficient	Multi inefficient
BS1	DMU7 DMU12	BS1	DMU7 DMU12	DMU12	DMU7
BS2	DMU18 DMU24 DMU25	BS1+BS2	DMU7 DMU12	DMU12	DMU7
BS3	DMU30 DMU37	BS1+BS2+BS3	DMU7 DMU12	DMU12	DMU7
BS4	DMU41 DMU52	BS1+BS2+BS3+BS4	DMU12 DMU41 DMU52	DMU12	–
BS5	DMU59 DMU66	BS1+BS2+BS3+BS4+BS5	DMU12 DMU41 DMU52	DMU12	–
BS6	DMU67	BS1+BS2+BS3+BS4+BS5+BS6	DMU12 DMU41 DMU52	DMU12	–

In conclusion, based on the numerical example, the following three definitions are provided:

– Definition 1: When a DMU is analysed in relation to other units in a bigger set, the DMU efficiency numerical value is smaller or equal to the efficiency obtained when a DMU is analysed in relation to other units in a smaller set. The estimation by the Multiset DEA analysis in a wider set is more restrictive than the evaluation by the monoset approach: $Eff^{\text{multiset}} \leq Eff^{\text{set}}$.

– Definition 2: When a DMU is analysed in relation to other units in an aggregate set, the number of efficient units is smaller than the total number of efficient units when units are analysed in relation to other units within the basic set:

$$N_{\text{EffDMU}}^{\text{multiset}} \leq \sum N_{\text{EffDMU}}^{\text{set}}$$

– Definition 3: Multiset efficient unit is efficient in both a basic set and a superset: $\text{Eff}_{\text{MSEff}} = 1(\text{BS}, \text{SS})$.

Additional clarification of efficiency, apart from the numerical value of efficiency, also includes the number of decision making units of the analysed set. It is a kind of weighted efficiency according to which efficient units are different and therefore comparable.

Conclusion

After reading the papers of the first and subsequent authors on the subject of the DEA method, it can be learnt that efficiency is a relative feature, as it varies depending on the data analysed. Additionally, the fact that this change may not only be positive (from inefficient to efficient unit), but also a negative one (from efficient to inefficient) has been ignored. Hence, the result of efficiency is only an estimate, and not an evaluation, that is, a final approximate value of efficiency.

With such more profound knowledge in mind, the objective of this paper is to acknowledge potentially inefficient units in order to avoid the previously stated negative process (efficient – inefficient), and sustain efficiency in such a way. In this regard, the Multiset DEA analysis has been proposed, which has also been explained from the theoretical point of view and practically illustrated, while in the end the research results were presented.

Theoretically, the Multiset DEA analysis is a mathematical way of calculating the efficiency of business operations of entities from different areas. The efficiency evaluations obtained by the Multiset analysis are re-evaluated, whereby new estimations of efficiency are equal or smaller than the previous ones, which implies very important information on potentially inefficient units.

Practically, the Multiset DEA analysis is illustrated at an actual example of Serbian railway passenger stations, which are an important part of both the railway segment and the environment. As a part of the changing environment, military sector is a more or less significant customer of transport services. We would like to mention in our paper the best practice units, Pančevački Most (DMU7) and Požarevac (DMU12) stations, within the Passenger Transport Section Belgrade, as well as Požarevac, Novi Sad and Indjija within the Passenger Transport Sector. The stated stations are: (i) an actually achievable model for inefficient units, (ii) a "live" proof of potential efficiency, and (iii) a confirmation of the application of the DEA method. The Požarevac station is a multiset

efficient station, as it is efficient in the Sector, while DMU7 is potentially inefficient as it becomes inefficient in the Sector.

Based on the results, with certain units we expect a negative process (efficient→multineffecinet). Now that we know what awaits us, our future research will definitively be the Sensitivity analysis. This is the logical order (or a post DEA analysis) as it provides concrete target values of input-output parameters (smaller inputs and/or higher outputs), which is necessary to realise in practice so that multiinefficient units can become multi-efficient. Targeted activities are different in each iteration and every time, and in any larger set. There is no doubt that with them in the future, efficient units of the basic set become stable, and they remain as efficient in the end as in the beginning. Therefore, the actual efficiency indicator is not only a pure numerical value, but also the number of units included in the analysis, which makes efficiency additionally defined. The extension of the case would include new inputs and outputs as characteristics of other subsystems, i.e. an analysis of the so-called DAT approach using sets and systems.

Additionally, future research refers to providing measures which encourage activities, and then measures possible to apply in concrete conditions. Now we will make a general proposal for better conversion input/output:

- New rational technology for the operation of stations (rational number of station personnel, rational redistribution of work, modernisation of operations, etc.);
- New rational organisation of railway transport (rational number of shares i.e. fewer trains, more departures, fewer "empty" lines, shorter stays and turning and line stations, which is to be achieved by a quality made timetables, etc.);
- Improved quality of transport service (timely departures, regular trains, comfort, providing information to passengers, travel without changing trains, accessibility of stations, diverse fee-related benefits etc.).

According to the presented system and the analogy to the case shown, the efficiency of entities from other activities may also be calculated, with completely different types of data (apart from the applied traffic-transport and demographic, economic and other statistical data). In the spirit of this magazine, we will mention organisational units, institutions and individuals of the Serbian Army, which is, similarly to the railway, a significant and complex, and above all, extremely important organisational system.

Through constant innovation lasting for a number of decades, the DEA model of mathematical programming has become a subject of significant and important number of works which present the modified models and contemporary examples. In terms of such tendency, the presented subject of DEA is not a completely closed issue, but it instead eagerly waits for new ideas and new examples, all with a wider comprehension of the notion of efficiency.

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ПЕРЕДОВАЯ ПРАКТИКА В КАЧЕСТВЕ РЕАЛИСТИЧНОГО И
ОТНОСИТЕЛЬНОГО ПРИМЕРА ДЛЯ ПОДРАЖАНИЯ ДЛЯ
НЕЭФФЕКТИВНЫХ ЕДИНИЦ: МУЛЬТИ-МНОЖЕСТВЕННЫЙ АОД
АНАЛИЗ

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ЯЗЫК СТАТЬИ: английский

Резюме:

Исследования эффективности единиц принятия решения в настоящей работе проводились в следующем направлении: эффективная→мульти-неэффективная→мульти-эффективная единица. Следовательно, цель настоящей работы – предусмотреть несколько шагов заранее, таких как: (1) идентификация "скрытых" неэффективных единиц в мульти-множестве, среди эффективных единиц в основном множестве, (2) осуществление эффективности в случаях идентифицированных неэффективных единиц. Таким образом указывается (предупреждается!) на отрицательный процесс эффективная→неэффективная, и создается возможность для своевременного реагирования, в том числе и для предупреждения мульти-неэффективности. Конкретной целью настоящей работы является оценка эффективности сербских вокзалов и железнодорожных пассажирских станций, прежде всего в основном

множестве Секции пассажирского транспорта Белград, а затем в мульти-множестве Секции пассажирского транспорта, и в конце в надмножестве – Секторе пассажирского транспорта. Это осуществляется с помощью применения мульти-множественного АОД метода (Анализ охвата данных), который представляет собой систему: (и) оценки относительной эффективности, в первой итерации, путем анализа основного множества, (ii) снижения эффективности потенциально неэффективных единиц, в последующих итерациях, путем анализа мульти-множества. В результате – эффективные станции Пожаревац и Панчевачки мост находятся на начальном уровне, а (ново)эффективные Пожаревац, Нови Сад и Инджия, на последнем уровне. Станция Пожаревац на практике остается лучшей станцией, и по своей мульти-эффективности является примером для подражания неэффективным единицам. Можно сделать вывод, что решение мульти-множественного АОД анализа в большей степени реалистично и в меньшей степени относительно, поскольку применимо к более широкому анализируемому множеству единиц принятия решения, то есть к большему охвату рассмотрения проблемы. Данные показатели являются весьма значимыми, особенно, если учитывать тенденции возрастающей глобализации, в данной связи мы рекомендуем интегральный мульти-множественный подход, в отличии от индивидуального единично-множественного подхода.

Ключевые слова: эффективность, анализ среды функционирования, мульти-множественный анализ, железнодорожные станции.

НАЈБОЉА ПРАКСА КАО РЕАЛАН И РЕЛАТИВАН УЗОР НЕЕФИКАСНИМ ЈЕДИНИЦАМА: МУЛТИСКУПОВНА ДЕА АНАЛИЗА

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ОБЛАСТ: математика, логистика, саобраћај
ВРСТА ЧЛАНКА: оригинални научни чланак
ЈЕЗИК ЧЛАНКА: енглески

Сажетак:

Правац истраживања ефикасности јединица одлучивања у овом раду јесте ефикасна→мултинеефикасна→мултиефикасна јединица, а општи циљ су два корака напред: (1) откривање „скривених” неефикасних јединица у мултискупу, међу ефикасним јединицама у основном скупу и (2) постизање ефикасности код

откривених неефикасних јединица. Тиме се указује (упозорава!) на негативан процес ефикасна→неефикасна, како би се правовремено реаговало и тиме предупредила мултинеефикасност. Конкретни циљ јесте да се процени ефикасност железничких путничких станица у Србији, најпре у основном скупу Секције за превоз путника Београд, затим у мултискупу Секција за превоз путника и, на крају, у надскупу Сектор за превоз путника. То се постиже мултискуповном методом ДЕА (Data Envelopment Analysis), што је систем за: (и) процењивање релативне ефикасности, у првој итерацији, анализом основног скупа, (ии) смањење ефикасности потенцијално неефикасних јединица, у наредним итерацијама, анализом мултискупа. Резултат је да су ефикасне станице Пожаревац и Панчевачки мост на почетном нивоу, а (ново)ефикасне Пожаревац, Нови Сад и Инђија на крајњем нивоу. Најбоља пракса је у станици Пожаревац, која је мултиефикасна и представља узор неефикасним јединицама. Закључује се да је решење мултискуповне ДЕА анализе више реално, а мање релативно, јер важи за шири анализирани скуп јединица одлучивања, тј. већи обухват сагледавања проблема. То је значајно за уклапање у ново доба растуће глобализације, те је наша препорука целовит мултискуповни приступ насупрот појединачном монокуповном приступу.

Кључне речи: ефикасност, Data Envelopment Analysis, мултискуповна анализа, железничке станице.

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