Simulation Studies of Combustion in Spark Ignition Engine using Openfoam

Lucky Anetor

Department of Mech. Engineering
Nigerian Defence Academy
Kaduna,
Nigeria

Edward E. Osakue

Department of Industrial Technology
Texas Southern University
Houston, Texas,
USA

Kendall Harris

Provost & Vice President for Academic
Affairs
Texas Southern University
Houston, Texas,
USA

The open source Field Operation and Manipulation (OpenFOAM) software was used to investigate the performance of a fully premixed, modern high-performance 4-valve, iso-octane, dual overhead cam (DOHC) engine with quasi-symmetric pent roof combustion chamber running at 1500 revolutions per minute. The peak pressure occurred at the TDC and had a value of about 30 bar. The results from this study show that the maximum combustion temperature occurred at approximately 95 degrees crank angle ATDC and has a volume averaged value of about 2700°K, whereas the actual computed peak temperature was found to be about 3000°K and it occurred at grid point 12630. The other temperatures which were found to be higher than the volume averaged temperature were found to be in the range 2968.81°K to 2974.01°K and correspond to grid point positions 12630 to 12633. The flame-wrinkling factor, $\Xi = S_t / S_u$ was found to be in the range $1.0 \leq \Xi \leq 3.8$. The dynamics of the regress variable b was accurately predicted.

Keywords: Premixed turbulent combustion, equivalence ratio, PISO, SIMPLE, PIMPLE, OpenFOAM

1. INTRODUCTION

There is presently increasing concern regarding environmental pollutions (greenhouse gas emissions, various oxides of nitrogen, particulate matters, etc.) originating from the operation of internal combustion engines. In view of this, stringent emission control laws are being promulgated by various Environmental Protections Agencies (EPAs). Consequently, there is an urgent need to control automotive contributions to urban air pollution and to achieve significant improvements in internal combustion engine (ICE) fuel economy. As a result of these stringent emission control laws and standards, research efforts have led to significant reductions in emissions from gasoline and diesel engines. In spite of the advent of new power sources such as hybrid electric vehicle (HEV), plug-in hybrid electric vehicle (PHEV), fuel cell, etc., for powering the automobile, it is worth mentioning that these prime movers still require augmentation with internal combustion engines with specific characteristics in order to improve their efficiencies.

Even though the electric vehicle is gradually making in-road as an alternative or possible replacement for the internal combustion engine, the complete realization of this prospect is presently not certain.

In view of the uncertainty surrounding having one hundred percent electric vehicle and the thought that after more than a century of development of the internal combustion engine a lot of prospect for further

development still exists. It is worth emphasizing that, there are a lot of empirical evidences which show that as the gasoline and diesel engine technology evolves, they continue to show substantial improvements in efficiency, power-density, improved emission and operational capacity.

In order to comply with the aforementioned stringent regulatory controls, research efforts which are geared towards clean diesel and gasoline engines are fundamental in guiding the development of new generation internal combustion engines. Advances in cleaner and more efficient combustion are as vital as other parameters such as alternative fuels, improved catalyst technologies or electronically controlled fuel injectors. Research activities relating to clean combustion require a comprehensive understanding of fluid dynamics, reaction kinetics, heat transfer, turbulent combustion and their interactions within the combustion chamber of an internal combustion engine.

Recent developments in combustion modeling have greatly improved the quality of internal combustion engine simulations. Furthermore, the complex dynamics /physics of combustion kinetics, pollutant formation, interaction of turbulence phenomena with other physical processes can now be modeled and analyzed. Modeling of reaction kinetics in turbulent combustion has advanced remarkably with efficient techniques, such as, the intrinsic low dimensional manifold [1], the flame prolongation of low dimensional manifold [2], the flame generated manifold [3] or the in-situ adaptive tabulation [4]. With these techniques it is now possible to comprehensively describe reaction kinetics during the combustion process, where hundreds of species and thousands of reactions are the norm. In addition to the aforementioned techniques, sophisticated approaches

---

Received: January 2020, Accepted: July 2020

Correspondence to: Prof. Lucky Anetor,
Department of Mechanical Engineering,
Nigerian Defence Academy, Kaduna, Nigeria
E-mail: lucky.anetor@tsu.edu

doi: 10.5937/fme2004787A

© Faculty of Mechanical Engineering, Belgrade. All rights reserved

FME Transactions (2020) 48, 787-799 **787**

such as the G-equations [5], flame surface density [6, 7], artificial flame thickening [8, 9, 10] or conditional moment closure [11, 12] are presently been employed to accurately predict flame propagation under the influence of turbulence. In spite of the attendant issues associated with in-cylinder flow and combustion, the Large Eddy Simulation (LES) of internal combustion engine is also being used to analyze a variety of complex issues like NO_x formation [13], cycle-to-cycle variations [14, 15] and flame-acoustics interactions [16, 17]. As long as the demands for low emissions, higher efficiency and improved fuel economy of the internal combustion engine continues, research efforts into the mathematical and numerical techniques for modeling turbulent combustion and associated complex physical phenomena will continue to be of vital interest to engine manufacturers and the engine research community.

In general, two main approaches are usually used for conducting research aimed at exploring ways of optimizing engine design and operation. These methods are experimental techniques which entail building of a real prototype engine and testing it while the other involves numerical simulation of the various engine processes. Because neither of these approaches is able to fully capture all the relevant dynamics at play in an internal combustion engine, the symbiotic relationship existing between them is usually taken advantage of during engine optimization projects. The experimentalist is unaware of the micro details of the physical processes within the engine combustion chamber. The experimentalist only has a macro knowledge of important parameters like global averaged temperature, pressure, etc., whereas the modeler is uncertain about the accuracy of the predicted results. The dilemma that was just pointed out is usually resolved by using the experimental data to validate the modeling results. Once the modeling results have been successfully validated, they can then be used to explore conceptual engines and combustion modes prior to building any real prototypes. Moreover, validated numerical simulations can also be used for parametric studies with the concomitant benefit of savings in time and cost.

As a result of the foregoing, the open source Field Operation and Manipulation (OpenFOAM) was used to investigate the performance of a fully premixed modern, high-performance 4-valve, iso-octane, dual overhead cam (DOHC) engine with quasi-symmetric pent roof combustion chamber running at 1500 revolutions per minute.

The unique aspect of this study is the fact that, the OpenFOAM was used to exhaustively investigate the salient operating characteristics (pressure, temperature, flame-wrinkling factor, $\Xi = S_t / S_u$, turbulent kinetic energy, regress variable, etc.) of an internal combustion engine.

This study is structured as follows: section 2 provides a brief description of the Open source Field Operation And Manipulation (OpenFOAM), which is the numerical code that was used for this work. Section 3 presents a brief fundamental philosophy underpinning the design of the OpenFOAM. In section 4, the models characterizing the dynamics of turbulent and chemically reactive flows within the combustion chamber of internal combustion engine are presented. Section 5

describes the premixed turbulent combustion model that was employed in this study. The computational and numerical schemes were presented in sections 6 and 7 respectively. The computational domain, grid and boundary conditions were presented in section 8. The results and discussions of the in-cylinder flow parameters and the combustion process of an ICE were presented in section 9. The conclusion of the present study was given in section 10.

2. DESCRIPTION OF OPENFOAM

The OpenFOAM numerical simulation code is a versatile tool which is gaining popularity and it is extensively being used for research and process improvements in the scientific and industrial environments. OpenFOAM implements operator-based implicit and explicit second- and fourth-order Finite Volume (FV) discretization in three-dimension and on curved surfaces, a second order Finite Element Method (FEM) solver and a particle tracking model. Flexibility in mesh management is realized by supporting un-structured polyhedral meshes and topological variations. Efficiency of execution is accomplished by the use of preconditioned Conjugate Gradient and Algebraic Multigrid solvers and the use of massively parallel computers in domain decomposition mode. Automatic mesh motion solver, where point motion is defined by only prescribing the boundary motion facilitates the setup of deforming mesh simulations.

The consistent object-oriented architecture of the code and the extensive number of available physical and numerical models recommends it as an excellent tool suitable for the simulation of complex problems.

3. EQUATION REPRESENTATION

The fundamental philosophy of the OpenFOAM design is that the solver applications are written using the OpenFOAM classes and have a syntax that closely looks like the partial differential equations being solved.

For example, the material or Lagrangian derivative, describing the rate of change of an intensive physical property $\phi(t)$ in time can be written as:

$$\frac{\partial \rho \vec{u}}{\partial t} + \nabla \cdot \phi \vec{u} - \nabla \cdot \mu \nabla \vec{u} = -\nabla p \quad (1)$$

which would have the OpenFOAM syntax given in Equation (2) below;

$$\begin{aligned} &\text{solve} \\ & (\\ & \text{fvm} :: \text{ddt}(\rho, U) + \text{fvm} :: \text{div}(\phi, U) - \\ & -\text{fvm} :: \text{laplacian}(\mu, U) \\ & \quad \quad \quad = -\text{fvc} :: \text{grad}(p) \\ &); \end{aligned} \quad (2)$$

4. GOVERNING EQUATIONS

The governing equations presented in this section deal with the phenomena of continuum mechanics. The

characteristic length- and time-scales of such problems are significantly (many orders of magnitude) greater than the scales of the discrete micro-structure of the types of matter present in the combustion chamber of internal combustion engine during operation. In view of this, any macroscopic physical property of matter, such as temperature $T(\vec{r}, t)$ pressure $p(\vec{r}, t)$, mass fraction $Y(\vec{r}, t)$, etc. can be characterized as a continuous function in macroscopic coordinates of space, $\vec{r}$ and time, t .

For compactness these equations are written in vector notations. The unit vectors in the x, y and z directions are denoted by $\vec{i}$, $\vec{j}$ and $\vec{k}$ respectively.

The position vector $\vec{r}$ is defined as:

$$\vec{r} = x\vec{i} + y\vec{j} + z\vec{k} \quad (3)$$

the vector operator ∇ is given by:

$$\nabla = \vec{i} \frac{\partial}{\partial x} + \vec{j} \frac{\partial}{\partial y} + \vec{k} \frac{\partial}{\partial z} \quad (4)$$

and the fluid velocity vector $\vec{u}$ is given by:

$$\vec{u} = u(x, y, z, t)\vec{i} + v(x, y, z, t)\vec{j} + w(x, y, z, t)\vec{k} \quad (5)$$

In order to simulate the dynamics of the processes prevailing inside the combustion chamber of a spark ignition engine, the conservative/transport equations of continuity, momentum, energy and other physical models such as combustion, heat transfer, equation of state, turbulence, etc. must be solved. These equations and the relevant sub-models or constitutive equations for Newtonian fluids are used in the present study and they are given below:

4.1 Continuity Equation

The continuity equation for species m can be written as:

$$\frac{\partial \rho_m}{\partial t} + \nabla \cdot (\rho_m \vec{u}) = \nabla \cdot \left[\rho D \nabla \left(\frac{\rho_m}{\rho} \right) \right] + \dot{\rho}_m^c \quad (6)$$

where ρ_m is the mass density of species m , ρ is the total mass density and $\vec{u}$ is the fluid velocity. D is the coefficient of diffusion and it is assumed to be governed by Fick's Law of diffusion. The constitutive relations for $\dot{\rho}_m^c$ the source term due to chemistry and D are given below.

By summing Equation (6) over all species the total fluid density equation becomes:

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \vec{u}) = 0 \quad (7)$$

since mass is conserved in chemical reactions.

4.2 Momentum equation

The momentum equation for the fluid mixture is given by:

$$\begin{aligned} \frac{\partial (\rho \vec{u})}{\partial t} + \nabla \cdot (\rho \vec{u} \vec{u}) = \\ = -\nabla p - \nabla \cdot \left(\frac{2}{3} \rho k \right) + \\ + \nabla \cdot \tilde{\sigma} + \rho \vec{g} \end{aligned} \quad (8)$$

where p is the fluid pressure.

The viscous stress tensor $\tilde{\sigma}$ is Newtonian in form, therefore;

$$\tilde{\sigma} = \mu_{eff} \left[\nabla \vec{u} + (\nabla \vec{u})^\tau \right] + \lambda \nabla \cdot \vec{u} \tilde{I} \quad (9)$$

The first and second coefficients of viscosity μ_{eff} and λ are defined below. The superscript τ denotes the transpose operator and $\tilde{I}$ is the unit dyadic. The specific body force $\vec{g}$ is assumed constant.

4.3 Turbulent Kinetic Energy and Dissipation Models

The kinematic eddy viscosity μ_{eff} can be evaluated in various ways, ranging from algebraic relations and local equilibrium assumptions to the solution of transport equations. The commonest method is to express μ_{eff} as a function of the turbulent kinetic energy k and its dissipation rate ε leading to a two-equation turbulence model. Accordingly, the transport equations for the turbulence kinetic energy, k and its dissipation rate, ε are:

$$\begin{aligned} \frac{\partial (\rho k)}{\partial t} + \nabla \cdot (\rho \vec{u} k) = - \left(\frac{2}{3} \rho k \right) \nabla \cdot \vec{u} + \\ + \tilde{\sigma} : \nabla \vec{u} + \nabla \cdot \left[\left(\frac{\mu_{eff}}{Pr_k} \right) \nabla k \right] - \rho \varepsilon \end{aligned} \quad (10)$$

and

$$\begin{aligned} \frac{\partial (\rho \varepsilon)}{\partial t} + \nabla \cdot (\rho \vec{u} \varepsilon) = - \left(\frac{2}{3} c_{\varepsilon 1} - c_{\varepsilon 3} \right) \rho \varepsilon \nabla \cdot \vec{u} + \\ + \nabla \cdot \left[\left(\frac{\mu_{eff}}{Pr_\varepsilon} \right) \nabla \varepsilon \right] + \frac{\varepsilon}{k} \left[c_{\varepsilon 1} \tilde{\sigma} : \nabla \vec{u} - c_{\varepsilon 2} \rho \varepsilon \right] \end{aligned} \quad (11)$$

Equations (10) and (11) are the standard $k - \varepsilon$ model with some additional terms. The source term $\left(c_{\varepsilon 3} - \frac{2}{3} c_{\varepsilon 1} \right) \rho \varepsilon \nabla \cdot \vec{u}$ in the ε - equation accounts for length scale changes when there is velocity dilation.

The quantities $c_{\varepsilon 1}, c_{\varepsilon 2}, c_{\varepsilon 3}, Pr_k$ and Pr_ε are constants whose values are 1.44, 1.92, -1.0, 1.5, 1.0 and 1.3 respectively. They are determined from experiments and other theoretical considerations.

The physical meaning of the various terms in Equation (10) is as follows; the term $\partial(\rho k)/\partial t$ represents the time rate of change of turbulent kinetic energy, $\nabla \cdot (\rho \vec{u} k)$ represents convection of turbulence by the resolved velocity field. The term $(-2/3) \rho k \nabla \cdot \vec{u}$ is a compressibility term that represents turbulent analogy of

pdV work. The term $\tilde{\sigma} : \nabla \bar{u}$ represents the production of turbulence by shear in the resolved velocity field and $\nabla \cdot \left[(\mu_{eff} / Pr_k) \nabla k \right]$ represents the self-diffusion of turbulence with a diffusivity of μ_{eff}/ρ . The term $-\rho\varepsilon$ represents the decay of turbulence into thermal energy. The physical meaning of the various terms in the rate of turbulence dissipation, that is Equation (11) are analogously defined.

4.4 Internal energy

The internal energy equation is given by:

$$\frac{\partial(\rho I)}{\partial t} + \nabla \cdot (\rho \bar{u} I) = -p \nabla \cdot \bar{u} - \nabla \cdot \bar{J} + \rho \varepsilon + \dot{Q}^c \quad (12)$$

where I is the specific internal energy, without the chemical energy. The heat flux vector $\bar{J}$ is the sum of contributions due to heat conduction and enthalpy diffusion, and it is given by:

$$\bar{J} = -K \nabla T - \rho D \sum_m h_m \nabla (\rho_m / \rho) \quad (13)$$

where T is the fluid temperature and h_m the specific enthalpy of species m . The source term due to chemical heat release $\dot{Q}^c$ is defined below.

4.5 Equations of state

The state constitutive equations are assumed to be those of an ideal gas mixture.

Therefore:

$$p = R_0 T \sum_m (\rho_m / W_m) \quad (14)$$

$$I(T) = \sum_m (\rho_m / \rho) I_m(T) \quad (15)$$

$$c_p(T) = \sum_m (\rho_m / \rho) c_{pm}(T) \cdot \frac{c_{pm}^0}{R_0} = a_{1m} + a_{2m} T_m + a_{3m} T_m^2 + a_{4m} T_m^3 + a_{5m} T_m^4 \quad (16)$$

$$h_m(T) = I_m(T) + R_0 T / W_m \Rightarrow \frac{h_{pm}^0}{R_0 T_m} \quad (17)$$

$$= a_{1m} + \frac{a_{2m}}{2} T_m + \frac{a_{3m}}{3} T_m^2 + \frac{a_{4m}}{4} T_m^3 + \frac{a_{5m}}{5} T_m^4 + \frac{a_{6m}}{6} \frac{s_m^0}{R_0} = a_{1m} \ln T_m + a_{2m} T_m + \frac{a_{3m}}{2} T_m^2 + \frac{a_{4m}}{3} T_m^3 + \frac{a_{5m}}{4} T_m^4 + a_{7m} \quad (18)$$

where o means standard state based on pressure (in the present study, pressure = 1 atmosphere), R_0 is the universal gas constant, W_m is the molecular weight of species m , $I_m(T)$ the specific internal energy of species m , c_{pm} is the specific heat coefficient at constant pressure of species m and s_m^0 is the specific entropy. The coefficients of $h_m(T)$, $c_{pm}(T)$ and s_m^0 are taken from JANAF Tables [18].

4.6 Chemical reaction

The chemical reactions occurring in the combustion chamber are modeled as:

$$\sum_m a_{mr} X_m \Leftrightarrow \sum_m b_{mr} X_m \quad (19)$$

Where X_m represents one mole of species m and a_{mr} and b_{mr} are integral stoichiometric coefficients for reaction r . The stoichiometric reaction coefficients must satisfy:

$$\sum_m (a_{mr} - b_{mr}) W_m = 0 \quad (20)$$

So that mass is conserved in the chemical reactions. The chemical reactions are divided into two classes, namely, those that proceed kinetically and those that are assumed to be in equilibrium.

Kinetic reaction r proceeds at a rate $\dot{\omega}_r$ which is given by:

$$\dot{\omega}_r = k_{fr} \prod_m (\rho_m / W_m)^{a'_{mr}} - k_{br} \prod_m (\rho_m / W_m)^{b'_{mr}} \quad (21)$$

The reaction orders are a'_{mr} and b'_{mr} and they are not necessarily equal to a_{mr} and b_{mr} . Therefore, empirical reaction orders can be used. The coefficients k_{fr} and k_{br} are assumed to be of a generalized Arrhenius form:

$$k_{fr} = A_{fr} T^{\xi_{fr}} \exp(-E_{fr} / T) \quad (22)$$

and,

$$k_{br} = A_{br} T^{\xi_{br}} \exp(-E_{br} / T) \quad (23)$$

where E_{fr} and E_{br} are activation temperatures.

The rates of equilibrium reactions are implicitly determined by the constraint conditions:

$$K_c^r(T) = \prod_m (\rho_m / W_m)^{(b_{mr} - a_{mr})} \quad (24)$$

where $K_c^r(T)$ the concentration equilibrium constant is assumed have the form:

$$K_c^r(T) = \exp(A_r \ln T_A + B_r / T_A) + C_r + D_r \cdot T_A + E_r \cdot T_A^2 \quad (25)$$

where $T_A = T/1000$ K.

From the foregoing, the reaction rates $\dot{\omega}_r$ is determined by Equation (20) or (21), the chemical source term in the species continuity equation is given by:

$$\dot{\rho}_m^c = W_m \sum_m (a_{mr} - b_{mr}) \dot{\omega}_r \quad (26)$$

and the chemical heat release term in the energy equation is given by:

$$\dot{Q}^c = \sum_r Q_r \dot{\omega}_r \quad (27)$$

where Q_r is the negative of the heat of reaction at absolute temperature zero.

$$Q_r = \sum_m (a_{mr} - b_{mr}) (\Delta h_f^0)_m \quad (28)$$

and $(\Delta h_f^0)_m$ is the heat of formation of species m at absolute temperature zero.

The transport coefficients in the equations above are:

$$\mu = \mu_{air} + c_\mu k^2 / \epsilon \quad (29)$$

$$\lambda = A_3 \mu \quad (30)$$

$$K = \frac{\mu c_p}{Pr} \quad (31)$$

and

$$D = \frac{\mu}{\rho Sc} \quad (32)$$

c_μ is an empirical constant with a standard value of 0.09. A Sutherland formula is used for μ_{air} as follows:

$$\mu_{air} = \frac{A_1 T^{3/2}}{T + A_2} \quad (33)$$

where A_1 and A_2 are constants. The constant A_3 is taken to be $(-2/3)$ in the calculation of turbulent flow. Pr and Sc are the Prandtl and Schmidt numbers and they are input constants.

5. PREMIXED TURBULENT COMBUSTION MODEL

The reactive processes taking place inside the combustion chamber of a spark ignition engine are highly complex and turbulent. Active research efforts aimed at understanding these physical processes are presently ongoing and one vital aspect of it is the search for numerical models which adequately and satisfactorily describe the processes involved. It is worth mentioning that the models should provide a better understanding of the processes involved, and provide the ability to predict the behavior of the combustion processes prevalent in the combustion chamber of spark ignition engines.

There are three categories of models which are often used to characterize the complex and turbulent nature of premixed combustion in spark ignition engines. They are the Eddy Break Up (EBU) [19], Thin Wrinkled Flame (TWF) [20, 21] and Flame Area Evolution (FAE) [22] models

In the Eddy Break Up model class the local burning rate is assumed to be controlled by small scale turbulent mixing with a characteristic time scale that is proportional to the turbulence dissipation scale. This proposition is incorrect and thus lead to concave flame front. For accurate near wall behavior the characteristic burn time should not be equated to the eddy turn over time $\tau_t = \kappa/\epsilon$ but derived from spectral descriptions of turbulence which takes into account the change in the spectrum of scales during flame kernel formation and on approaching a wall.

The Thin Wrinkled Flame models [23, 24] do account accurately for the normally thin (of the order of the Kolmogorov microscale) and wrinkled flame structure. The wrinkling being responsible for the increased burning rate over a smooth flame burning at laminar burning velocity. The laminar flamelet assumption has the advantage of making it possible to include detailed chemistry and flame straining effects in a more computationally efficient manner. However, these models assume that the characteristic scale of wrinkling is proportional to the characteristic turbulence scales thereby leading to the same issues affecting those of the Eddy Break Up model.

The more recently developed Flame Area Evolution models [25, 26] share some of the characteristics of the Thin Wrinkled Flame models such as the thin flame assumption and the laminar flamelet burning. The local wrinkled flame area is however, modeled by an evolution equation which allow incorporation of turbulence effects as well as effects generated by the flame itself and non-local effects [27]. This type of modeling has been found to produce realistic results in modeling combustion in spark ignition engines [28] where simulation of combustion was based on the Weller flame wrinkling model [27, 29]. It provides a transport equation for the spatial and temporal evolution of the wrinkling factor Ξ . The flame wrinkle density Ξ is the flame area per unit area resolved in the mean direction of propagation. The use of Ξ provides physical justification for modeling the velocity field generated by the combustion, rather than the traditional density weighted ensemble averaging and gradient transport modeling. Moreover, Ξ may be categorized as a spectral density function in length scale phase space, thereby enabling detailed description of the turbulent/flame interaction processes.

In the present work, the 2-equation Weller model for flame distribution, that is, the transport equation for the spatial and temporal evolution of progress variable b and governing equation for the wrinkling factor Ξ is used to model combustion.

In premixed combustion the flow field consists of regions of unburnt reactants and regions of burnt products. The extent of combustion of the air/fuel mixture can be described in a variety of ways in terms of a progress variable, c such that $0 \leq c \leq 1$, with the extremal values indicating the presence of unburnt or fully burnt mixture phases, and the transition between these extremal values marking the flame front. This can be linked directly to physical properties of the air/fuel mixture, for instance, by utilizing normalized temperature, T or product mass fraction, Y , as follows:

$$c = \frac{T - T_u}{T_B - T_u} \quad \text{or} \quad c = \frac{Y_p - Y_{p,u}}{Y_{p,B} - Y_{p,u}} \quad (34)$$

Irrespective of how the progress variable is defined, the exact relationship is not important; however, it can simply be viewed as an artifice for tracking the quantity of air/fuel mixture burned. In the present work, we will use a progress or regress variable, $b = 1 - c$; with $0 \leq b \leq 1$

1, where 0 and 1 represents unburnt and fully burnt air/fuel mixture respectively. Suffices B and u represents burned and unburned fuel-air charge.

In view of the foregoing, the models for the wrinkle density Ξ transport equation and the corresponding equation for the regress variable b which may be considered a normalized fuel concentration from its origins as a flame area model to a closed pair of coupled transport equations and simple one equation model derived therefrom are given below:

The simplified transport equation for Ξ is given by:

$$\beta = -0.22, f = 2.3, \Xi = 4.48 \quad (35)$$

$$(a) G = G\Xi - R \frac{\Xi_{eq} - 1}{\Xi_{eq}}, \quad (36)$$

$$(b) R = \frac{0.28}{\tau_\eta} \cdot \frac{\Xi_{eq}^*}{\Xi_{eq}^* - 1}$$

Since the solution of the spectral evolution equations coupled with Equation (36) is prohibitively expensive, simple algebraic equations are considered more appropriate. The approach used in the present study is based on flame speed correlation, Equation (37) of Gülder [30], which has proven to be very good when compared to the full spectral solutions is used in this study, and it is given in Equations (37a) and (37b).

$$(a) \Xi_{eq}^* = 1 - 0.62 \sqrt{\frac{u'}{S_{ub}}} \mathcal{R}_\eta, \quad (37)$$

$$(b) \Xi_{eq} = 1 + 2(1 - b)(\Xi_{eq}^* - 1)$$

where Ξ is the ratio of turbulent flame velocity to laminar flame velocity, $\Xi = S_t/S_{ub}$; S_t is the turbulent flame speed, S_{ub} is the laminar flame speed, τ_η is the Kolmogorov time-scale, u' is the subgrid turbulence intensity, $\bar{u}_s$ is the surface filtered velocity of the flame, $\mathcal{R}_\eta$ is the Kolmogorov Reynolds number, σ_s and σ_t and are the resolved strain rates.

The flame front propagation is modeled by solving a transport equation for the density-weighted mean reaction regress variable b as follows:

$$\frac{\partial(\rho b)}{\partial t} + \nabla \cdot (\rho \bar{u} b) - \nabla \cdot \left(\frac{\mu_t}{Sc_t} \nabla b \right) = -\rho_{ub} S_{ub} \Xi |\nabla b| \quad (38)$$

For the interested reader, the derivation of these models can be found in [2, 12, 15].

The final requirement for closure is to provide a model for the laminar flame speed S_{ub} . This will largely be dependent on the characteristics of the type of flame under consideration. Under certain circumstances it might be reasonable to assume that the laminar flame speed is unaffected by strain and curvature, therefore, we set $S_{ub} = S_{ub}^0$, the unstrained flame speed.

In the present study the laminar flame speed S_{ub} is used and it is computed using the Gülder's correlation [30] and it is given by:

$$S_{ub}(\Phi, T_{ub}, P_{ub}) = W \Phi^\eta \exp \left[-\xi (\Phi - 1.075)^2 \right] \left(\frac{T_{ub}}{T_0} \right)^\alpha \left(\frac{P_{ub}}{P_0} \right)^\beta \quad (39)$$

where P and T are the pressure and temperature respectively, Φ is the equivalent ratio. For gasoline (iso octane), $W = 0.4658$, $\eta = -0.326$, $\xi = 4.48$, $\alpha = 1.56$, $\beta = -0.22$, $f = 2.3$, $\Xi = 4.48$ and subscript ub represents unburned state.

It is worth mentioning however, that this approach has a drawback. In regions of high Damköhler, Da (highly reactive species) and Reynolds, Re numbers, the flame-sheet reaction zone is very thin and the transition of the progress variable is extremely steep. In view of this, the progress variable cannot be explicitly resolved on the large eddy simulation mesh. Sometimes, the Thickened Flame approach is employed to resolve this issue [24].

6. COMPUTATIONAL METHODOLOGY

In the present study, the reactive Reynolds Averaged Navier-Stokes (RANS) model (Equations (1) to (33)) and the $b - \Xi$ two-equation model (Equations (34) to (39)) were used to investigate the performance of a fully premixed modern, high-performance 4-valve, iso-octane, dual overhead cam (DOHC) engine with quasi-symmetric pent roof combustion chamber, running at 1500 revolutions per minute. The intake valves are canted -20° while the exhaust valves are canted $+22^\circ$. The evolution of turbulence inside the combustion chamber of the spark ignition engine was modeled using the standard $k - \varepsilon$ equation augmented with the wall functions.

The flame-wrinkling model that was used to model combustion in the present study was obtained by replacing Equation (35) with the equilibrium expression Equation (37) and using Gülder's correlation, that is, Equation (39) for calculating the laminar flame speed S_{ub} . Equations (35) and (37a) and (37b) are usually referred to as the one-equation and 2-equation Weller models respectively. The thermodynamical properties were calculated using the JANAF Tables [18]. The mixture was ignited at 15° Before Top Dead Center (BTDC).

The performance parameters investigated were the pressure p , temperature T , turbulence intensity u' , and the regress variable b . These parameters were investigated over the range of crank angle $-180 \leq \text{CA} \leq 120$ and air/fuel equivalence ratio, $\Phi = 1.0$.

6.1 Comments

a. Ξ may be obtained by either the solution of the Ξ transport equation or from an algebraic expression. Both methods are based on Gülder's flame speed correlation which has been shown to be appropriate by comparison with the results obtained from the spectral model.

b. Strain effects are incorporated directly into the Ξ equation but not in the algebraic approximation. More

work needs to be carried out on this chiefly because of the enhanced removal rate caused by flame compression. Analysis using results of the spectral model will be required.

c. For cases involving very lean propane flames or other flames which are very strain-sensitive, a transport equation for the laminar flame speed is required. This equation is derived using empirical arguments involving the strain time scale and the strain-rate at extinction. The transport velocity is the same as that for the Ξ equation [31].

7. NUMERICAL SCHEME

The governing Equations (1) to (39) were discretized both in space and time using the appropriate discretization utilities in OpenFOAM. Each of the term in these Equations is represented individually in OpenFOAM code using the classes of static functions finite Volume Method (fvm) and finite Volume Calculus (fvc) methods respectively. fvm and fvc contain static functions, representing differential operators, for example, ∇^2 , ∇ and $\partial/\partial t$, etc. that discretize **geometricField<Type>s**. The purpose of defining these functions within the two classes, namely, fvm and fvc, rather than one, is to distinguish:

- Functions of fvm that calculate implicit derivatives of and return an **fvmatrix<Type>** and,
- Some functions of fvc that calculate explicit derivatives and other explicit calculations, returning a **geometricField<Type>**.

Finite volume discretization of each term is formulated by first integrating the term over a cell volume V . Most spatial derivative terms are then converted to integrals over the cell surface S bounding the volume using Gauss's theorem:

$$\iiint \nabla \star \phi dV = \iint d\vec{S} \star \phi \quad (40)$$

where $\vec{S}$ is the surface area vector, $\square$ can represent any tensor field and the star notation $\star$ is used to represent any tensor product, such as, inner, outer and cross and the respective derivatives: divergence $\nabla \cdot \phi$, gradient $\nabla \phi$ and $\nabla \times \phi$. Volume and surface integrals are then linearized using appropriate schemes. The schemes which were used for each of the terms in Equations (1) to (39) are tabulated in Table 1.

Table 1: Discretization Scheme

Terms in Equations (1) to (39)	Numerical scheme
Time derivative	Implicit Euler
Convection	Gauss linear
Divergence	Gauss upwind
Laplacian	Gauss linear limited
Interpolation	Linear

Comprehensive details concerning these schemes can be found in [32].

8. CODE VALIDATION, COMPUTATIONAL DOMAIN, MESH AND BOUNDARY CONDITIONS

8.1 Code validation

The numerical schemes implemented in the OpenFOAM code have been extensively validated in the error estimation studies [33, 34] and comparisons with analytical solutions [31].

8.2 Computational domain and mesh

The computational domain over which solutions of the differential equations described in Equations (1) to (39) were solved are those lying between the cylinder surfaces, cylinder head and piston face. In computational fluid dynamics parlance, these surfaces are referred to as walls. In internal combustion engines two of these walls move - the piston face moves continuously in time and the valves move intermittently. If a finite-difference computational mesh which is fixed in space is used, much of the grid will not be utilized during parts of the piston cycle. A mesh which does not translate with the piston motion is therefore highly wasteful of computer resources, that is, both computer processing unit's (cpu's) time and storage memory. This problem was resolved by defining a mesh which translates with the motion of the piston such that the whole mesh is always confined between the cylinder and piston head. Various ways of accomplishing this have been proposed, but the Arbitrary Lagrangian-Eulerian (ALE) technique [35] has been found to be the most suitable. This is the method that was used in the present work.

The hexahedral computational mesh employed in this study was generated from the same data that was used for the KIVA-3V 4-valve model [36]. The initial computing mesh was created by the OpenFOAM's kivaToFoam grid conversion utility. The mesh at the bottom dead center ($180^\circ CA$ BTDC) position consists of a total number of 30742 nodes, 85742 faces, 79522 internal faces and 27544 hexahedral cells. The minimum and maximum face areas were $2.74725 \cdot 10^{-7}$ and $4.11662 \cdot 10^{-5} \text{ m}^2$, while the minimum, maximum and total volumes are $3.07069 \cdot 10^{-10}$, $1.36137 \cdot 10^{-7}$ and $1.31297 \cdot 10^{-4} \text{ m}^3$ respectively. The maximum skewness of the concerned face was 3.73901 which was adjudged satisfactory. It is worth mentioning that the OpenFOAM has a lot of utilities for managing the computational mesh, thereby affording the opportunity to building a more appropriate mesh and thus reducing and improving upon the discretization errors and the accuracy of the numerical results. Figures 1 and 2 show the computational mesh for the piston at the bottom dead center (BDC) and top dead center (TDC) positions respectively. The automatic mesh motion solver was used to compute the piston and valve motions. The characteristics of the computational mesh and intake swirl specification when valve geometry was not modeled but specified are shown in Tables 2 and 3.

Table 2. Characteristics of computational mesh

Patch	Boundary type	No. of nodes (n_p)	Number of faces/Start faces n_F/n_{SF}
Piston	Wall	1400	1326/79522
Cylinder liner	Wall	2858	2740/80848
Cylinder head	Wall	2260	2184/83558
Engine Mesh	Layered	For control of how engine mesh is to be treated during piston motion	

Table 2: Intake swirl specification when valve geometry was not modeled but specified

Swirl parameter	Value
Swirl axis	(0.0 0.0 0.1)
Swirl center	(0.0 0.0 0.056)
Swirl rpm ratio	2.0
Swirl profile	3.11

Figure 1: Computational mesh with the piston at BDC **Figure 2: Computational mesh with the piston at TDC** **Figure 3: Graph of the residual of the three velocity components and turbulent kinetic energy** **Figure 4: Graph of the residual of the regress variable**

8.3 Boundary conditions

In order to completely specify a numerical model, it is necessary to supply the conditions at the boundaries of the solution domain for the variables. These conditions are usually obtained either by specifying the value of the dependent variable at the boundary, or the value of the associated flux, or a relation between the two. The specifications of the relevant boundary conditions employed in this work also follow these basic principles. Accordingly, the boundary conditions are specified in Table 4.

Table 3: Initial boundary conditions

Parameter	Description	Initial condition
αt	Turbulence thermal diffusivity	Uniform internal field = 0
B	Regress variable	Uniform internal field = 1.0
K	Turbulence kinetic energy	Uniform internal field = 2.661
ε	Turbulence kinetic energy dissipation rate	Uniform internal field = 25.763
μ_t	Turbulence viscosity	Uniform internal field = 0
P	Kinematic pressure	Uniform internal field = 1.01325
S_u	Laminar flame speed	Uniform internal field = 0.434
T_u	Temperature	Uniform internal field = 450
T_w	Cylinder wall temperature	Uniform internal field = 450
$\vec{u}$	Velocity field	Uniform internal field = (0,0,0)
Ξ	Flame-wrinkling factor, S_r/S_u	Uniform internal field = 0.0

8.4 Initial conditions

The simulations were initialized at 180-degree *BTDC* and the air/fuel mixture is assumed to be at rest within the entire computation domain and calculations were terminated at 120-degree *ATDC*. The initial inlet temperature and pressure were set to 600°K and 1.9 bar and to a fixed value of 450°K at the walls respectively. The initial velocity distribution was assumed to vary linearly between the piston and the cylinder head, being zero at the cylinder head and equal to the piston speed at the piston head. Furthermore, the no-slip boundary conditions were imposed on the walls.

At the boundaries of the computational domain, heat and momentum losses were calculated by assuming that boundary layers were turbulent and matching to a law-of-the-wall velocity profile.

The initial turbulent kinetic energy was assumed to be uniform and equal to 10% of the square of the mean piston speed, while the initial turbulent length scale was assumed to be 40% of the distance from each of the cells closest to the solid boundary. At engine speed of 1500 revolutions per minute (4.1125 m/s), the initial

specific turbulent kinetic energy, $k = 2.661 \text{ m}^2/\text{s}^2$, while the initial rate of dissipation of turbulence kinetic energy $\varepsilon = 25.763 \text{ m}^2/\text{s}^2$, respectively.

Since there was no ignition initially, that is, at time, $\theta_{start} = 180^\circ \text{CA BTDC}$, we set the regress variable, $b = 1.0$ and the flame wrinkling factor, $\Xi = S_t/S_u = 1.0$ in the whole computational domain.

The complete initial conditions governing and controlling other parameters are summarized in Table 5 below:

Table 4: Initial conditions and Control parameters

Description	Parameter	Units	Value
Start time	θ_{start}	$^\circ \text{CA BTDC}$	-180
Regress variable	B	-	1.0
Flame wrinkling factor	Ξ	-	1.0
Max time interval	$\Delta\theta_{max}$	$^\circ \text{CA}$	1.0
Initial temperature of unburnt air/fuel	T_{ub}	K	450
Initial pressure of unburnt air/fuel	P_{ub}	Bar	1.01325
Time interval	$\Delta\theta$	$^\circ \text{CA}$	0.05
Write control interval	Output result interval	$^\circ \text{CA}$	5
Max Courant Number	Co	-	0.2
Stop time	θ_{fin}	$^\circ \text{CA ATDC}$	120

8.5 Solution procedure

The PIMPLE algorithm was used to solve discretized Equations (1) to (39). The PIMPLE numerical scheme is a combination of the pressure-implicit split-operator (PISO) and the semi-implicit method for pressure-linked equations (SIMPLE) algorithm. The PIMPLE algorithm is an iterative scheme which is normally used for solving the momentum and mass conservation equations. Details concerning the operation of PIMPLE can be found in [34]. However, it is worth mentioning that PIMPLE has two iterative mechanisms namely,

Outer Correctors and Inner Correctors. These iterative utilities ensure stability especially when dealing with large time steps where the maximum Courant number may consistently be greater than 1 or when the nature of the solution is inherently unstable.

In the present study, the Outer and Inner Correctors were set to 2, while the Non-Orthogonal Corrector was set to 1. The stability of the algorithm was further improved by setting the relaxation factor to 0.7. The tolerance and relative tolerance values which were used to signify solution convergence are tabulated in Table 6.

Table 5: Solver tolerance

Description	Parameter	Tolerance	Relative tolerance
Pressure	P	10^{-3}	10^{-1}
Velocity field	$\vec{u}$	10^{-3}	10^{-1}
Turbulence kinetic energy	K	10^{-3}	10^{-1}
Turbulence kinetic energy dissipation rate	E	10^{-3}	10^{-1}
Density	P	10^{-3}	10^{-1}
Regress variable	b	10^{-3}	10^{-1}
10^{-3} Flame-wrinkling factor, S_t/S_u	Ξ	10^{-3}	10^{-1}
Relaxation factor	ϕ	0.7	-

9. RESULTS AND DISCUSSIONS

The details of the engine specification, fuel and ignition characteristics that was used in the present study are provided in Tables 7 and 8 below. The finite-difference approximations to the governing Equations (1) to (39) were solved with the OpenFOAM XiEngineFoam solver for internal combustion engines.

Table 6: Engine specifications and fuel

Parameter	Value
Bore (mm)	92
Stroke (mm)	84.23
Clearance height (mm)	1.15
Crank radius (mm)	44.2
Connecting rod length (mm)	147
Clearance height (mm)	1.409
Minimum chamber volume (mm^3)	71.557
Maximum chamber volume (mm^3)	631.297
Compression ratio, r_c	8.82
Engine speed (rpm)	1500
Intake valves canted	-20°
Exhaust valves canted	$+22^\circ$
Intake pressure (bar)	1.9
Cylinder wall temperature, $T_w(K)$	600
Initial temperature, $T(K)$	600
Fuel, iso-octane	C_8H_{18}
Fuel-air equivalence ratio, Φ	$\Phi = 1$
Laminar flame speed (m/s)	0.43

The computational platform that was used to conduct the simulation studies was the Lenovo ThinkPad P50 Signature Edition with installed memory (RAM) capacity of 16.0 GB and the Intel Core i7-6700HQ CPU at 2.60 GHz processor. The installed operating system is CentOS Linux 7.4.1708 (based on the source code RHEL 7.4 distribution) for the x86_64 architecture. The compiler used was the 64-bit Intel Parallel Studio XE Compiler for Linux Operating System. The results of this study are depicted in Figures 3 to 12.

Table 7: Ignition Characteristics

Relative spark plug position from edge (x,y,z)m	(0.03, 0, 0.091)
Diameter (m)	0.002
Ignition sphere fraction (-)	1.0
Ignition thickness (m)	0.0
Ignition circle fraction	1.0
Ignition kernel area (m^2)	0.0
Start of ignition crank angle ($^\circ \text{CA BTDC}$)	-15
Duration ($^\circ \text{CA}$)	-20
Strength (mJ)	4.5

Figures 3 and 4 show the residuals of the velocity component in the x,y and z directions, turbulent kinetic energy and the regress variable respectively. The total number of iterations at which convergence was achieved for all the variables range from 5500 to 6000. In view of Figures 3 and 4, it safe to assume that the numerical scheme was well-behaved during the computation of the properties being investigated, that is, the mass continuity equation, temperature, pressure, regression variable, etc.

Figure 5 shows the variation of pressure with crank angle. As can be seen from Figure 5, the peak pressure occurred a few crank angle degree ATDC and has a value of about 30 bar.

Figure 5: Graph of pressure versus crank angle

The graph of volume averaged temperature versus crank angle is shown in Figure 6. Figure 6 shows that the maximum volume averaged combustion temperature occurred at approximately 95 degree crank angle ATDC and has a volume averaged value of about 2700°K, whereas the actual peak temperature was found to be 3000°K and it occurred at grid point 12630. The other temperatures within the combustion chamber which were higher than the volume averaged peak temperatures were found to be in the range 2968.81°K to 2974.01°K and corresponds to grid points in the range 12630 to 12633.

Figure 6: Graph of volume averaged temperature versus crank angle

It is worth mentioning that, either advancing (that is, taking the spark initiation further from the BTDC) or retarding the start of ignition (that is, taking the spark initiation closer to TDC) both have some benefits and disadvantages [37]. Advancing initiation of ignition increases the peak pressure within the engine combustion chamber, whereas retarding the start of ignition reduces the maximum pressure. Furthermore, advancing the spark timing increases the maximum temperature, while retarding initiation of reduces the peak temperature. The aforementioned characteristics show how retarding the initiation of spark can have a beneficial effect on NOx production while simultaneously reducing the tendency for the engine to knock. However, the life span of the exhaust valve could be adversely affected because retarding the ignition timing does increase the heat release temperature, but it could be useful in helping to achieve early catalyst light-off. Most importantly, retarding the ignition timing does decrease the power output with the concomitant reduction of cycle efficiency. Figures 5 and 6 show that the

locations of the peak pressure and temperature are not correlated, that is, the maximum pressure occurred at a few crank angle degree ATDC position whereas the peak temperature occurred at about 95° ATDC which corresponds to about 5 ms apart. The reason for this could be due to the fact that the computed values of temperature were volume averaged.

Figure 7 shows the variation of volume averaged turbulent kinetic energy/turbulent intensity with crank angle. It is worth noting that the graph shows two turning points. The maximum turbulent kinetic energy occurred at approximately 25 degree before the top dead center position and decreased to just below 1.2 m/s at the top dead center position. This could be due to the fact that turbulence is modified by flames (recall that ignition was initiated at 15-degree crank angle BTDC) through flow acceleration and changed kinematic viscosity. It is worth mentioning, however, that modified turbulence structure does alter the flame shape by wrinkling it thereby resulting in large flame area. The wrinkled and increased flame area has the overall effect of enhancing mixing and chemical reactions through temperature fluctuations. Furthermore, it is worth noting that as the power stroke continues, the turbulent kinetic energy continues to decrease in magnitude.

Figure 7: Graph of volume averaged turbulence intensity versus crank angle

Figure 8 shows the variation of the regress variable with crank angle. As expected, the regress variable maintained a constant value of 1.0 (unburnt air/fuel mixture) until about 10 degrees before the top dead center position. Thereafter, the air/fuel mixture was rapidly consumed.

Figures 9 to 12 show the combustion chamber volume distributions of pressure, temperature, turbulent kinetic energy and flame wrinkling fields at various grid points and crank angle positions stated in each of the figures.

Figure 9 shows the spatial distribution of pressure within the combustion chamber at the top dead center position. From the figure we can see that the pressure was almost uniform with a value of about 30 bar within the entire combustion chamber. The spatial variation of temperature versus crank angle at the TDC position is shown in Figure 10. We can see from Figure 10 that even though ignition was initiated at 15-degree BTDC, the flame kernel was not spreading as rapidly as expected. This could be attributed to the dissipation of turbulent intensity as depicted in Figure 7. Plotted in Figure 11 is the volume evolution of the turbulent kinetic energy at the TDC position. It can be observed that

the highest levels of turbulence are induced in the cylinder by the inflow around the valve and it occurs both off the near-side top surface and the far edge of the valve. From the figure we see that the intensity of turbulence is highest within the periphery of the combustion chambers.

Figure 8: Graph of volume averaged regress variable versus crank angle

Figure 9: Distribution of pressure at TDC

Figure 10: Distribution of volume averaged temperature at TDC

This is obviously due to the fact that piston motion is creating a lot of viscous shear, that is, large eddies of the order of integral length scale, l close to the combustion chamber walls. These large eddies in turn break into medium and smallest-scale turbulent eddies on the order of the Kolmogorov scale which then dissipates the turbulence energy via molecular viscosity. Figure 11

shows that the values of the volume averaged turbulent kinetic energy falls in the range $5.5 \cdot 10^{-3} \leq k \leq 3.8 \cdot 10^0$.

Figure 11: Distribution of turbulent kinetic energy at TDC

The distribution of flame wrinkling factor, Ξ at the top dead center position is shown in Figure 12. The figure shows that at the top dead center position, the flame-wrinkling factor, $\Xi = S_f/S_{ub}$ was in the range $1.0 \leq \Xi \leq 3.8$ which translates to a magnification factor of about 3.8 of the quiescent value. The resultant effect being a very impressive flame kernel size as can be seen from Figure 12.

Figure 12: Distribution of flame wrinkling factor at TDC

10. CONCLUSION

The open source Field Operation and Manipulation (OpenFOAM) software was used to investigate the performance of a fully premixed modern, high-performance 4-valve, iso-octane dual overhead cam (DOHC) engine with quasi-symmetric pent roof combustion chamber running at 1500 revolutions per minute. The numerical results were found to qualitatively reproduce the basic features that are usually observed in internal combustion engine test bed experiments. In the XiEngineFoam solver, the flame front propagation was modeled by regress variable b , with the relation $b = 1 - c$, where c is the progress variable. The flame propagation was modeled by solving transport equation of the regression variable, Equations (35) to (39).

In specific terms, the salient conclusions from this study can be summarized as follows:

1. The results of the present work were found to qualitatively reproduce the general characteristics of the pressure distribution which are similar to those usually occurring within combustion chamber of internal combustion engines. The peak pressure occurred at a few crank angle degree ATDC and has a value of about 30 bar.
2. The present study shows that the peak volume averaged temperature of about 2700°K was within the general ballpark value of temperatures that are usually prevalent within the combustion chamber of a spark ignition engine. It is worth mentioning that the combustion duration was also well within typical industry standard, however, the location of the peak temperature lagged behind that of the maximum pressure. The simulation also shows that the actual maximum temperature within the combustion chamber was 3000°K and it is located within a very small region inside the combustion chamber.
3. The flame-wrinkling factor, $\Xi = S_p/S_u$ was found to be in the range $1.0 \leq \Xi \leq 3.8$ which translates to a magnification of nearly four times that of the quiescent value.
4. The dynamics of the regress variable b was accurately predicted as shown in Figure 8.

ACKNOWLEDGEMENTS

The work reported herein was graciously supported by the Nigerian Defence Academy, Kaduna, Nigeria, and Texas Southern University, Houston, Texas, USA. The authors also wish to express their sincere gratitude to the reviewers for their insightful and constructive remarks, which led to improving the clarity of this paper considerably.

REFERENCES

- [1] Maas, U., Pope S. B., Implementation of simplified chemical kinetics based on intrinsic low-dimensional manifolds. Symposium (International) on Combustion. Vol. 24. 1. Elsevier. 1992, pp. 103–112.
- [2] Gicquel, O., Darabiha, N. Thevenin, D., Laminar premixed hydrogen/air counterflow flame simulations using flame prolongation of ILDM with differential diffusion. Proceedings of the Combustion Institute 28.2 (2000), pp. 1901–1908.
- [3] Van Oijen, J., Lammers, F. and De Goey, L., Modeling of complex premixed burner systems by using flamelet-generated manifolds. Combustion and Flame 127.3 (2001), pp. 2124–2134.
- [4] Yang, B., Pope, S., Treating chemistry in combustion with detailed mechanisms in situ adaptive tabulation in principal directions premixed combustion. Combustion and Flame 112.1 (1998), pp. 85–112.
- [5] Tan Z., Kong, S.C. and Reitz, R. D., Modeling premixed and direct injection SI engine combustion using the G-equation model. Tech. rep. SAE Technical Paper, 2003.
- [6] Cant, R., Pope, S., Bray, K., Modelling of flamelet Surface-to-volume Ratio in Turbulent Premixed Combustion. Symposium (International) on Combustion. Vol. 23. 1. Elsevier. 1991, pp. 809–815.
- [7] Muppala, Siva, Aluri, Naresh, Dinkelacker, Friedrich, Leipertz Alfred, Development of an Algebraic Reaction Rate Closure for the Numerical Calculation of Turbulent Premixed Methane, ethylene, and propane/air flames for pressures up to 1.0 MPa. Combustion and flame 140.4 (2005), pp. 257–266.
- [8] Kuenne, G., Ketelheun, A. and Janicka, J., LES modeling of premixed combustion using a thickened flame approach coupled with FGM tabulated chemistry. In: Combustion and Flame 158.9 (2011), pp. 1750–1767.
- [9] Proch, F. and Kempf, A., Modeling heat loss effects in the large eddy simulation of a model gas turbine combustor with premixed flamelet generated manifolds. In: Proceedings of the Combustion Institute 35.3 (2015), pp. 3337–3345.
- [10] Wang, G., Boileau, M., Veynante, D., Implementation of a dynamic thickened flame model for large eddy simulations of turbulent premixed combustion. In: Combustion and Flame 158.11 (2011), pp. 2199–2213.
- [11] Kim, S. H., K. Huh, Y., Tao, L., Application of the elliptic conditional moment closure model to a two-dimensional nonpremixed methanol bluff-body flame. In: Combustion and Flame 120.1 (2000), pp. 75–90.
- [12] Cha, C. M., Kosaly, G., and Pitsch, H., Modeling extinction and reignition in turbulent non-premixed combustion using a doubly-conditional moment closure approach. In: Physics of Fluids 13.12 (2001), pp. 3824–3834.
- [13] Lazik, W., Doerr, Th., Bake, S., Bank, R. and Rackwitz, L., Development of lean-burn low-NOx combustion technology at Rolls-Royce Deutschland, ASME Turbo Expo 2008: Power for Land, Sea, and Air, American Society of Mechanical Engineers. 2008, pp. 797–807.
- [14] Banerjee, S., Liang, T., Rutland, C., and Hu, B., Validation of an LES Multi Mode Combustion Model for Diesel Combustion, SAE Technical Paper 2010-01-0361, 2010, <https://doi.org/10.4271/2010-01-0361>.
- [15] Fontanesi, S., d'Adamo, A., Rutland, C. J., Large-eddy simulation analysis of spark configuration effect on cycle-to-cycle variability of combustion and knock. International Journal of Engine Research 16.3 (2015), pp. 403–418.
- [16] d'Adamo, A., Breda, S., Fontanesi, S., Cantore, G., LES Modelling of Spark-Ignition Cycle-to-Cycle Variability on a Highly Downsized DISI Engine, SAE Int. J. Engines 8(5):2029-2041, 2015, <https://doi.org/10.4271/2015-24-2403>. [69] P. Wolf et al. Acoustic and large eddy simulation studies of azimuthal modes in annular combustion chambers. Combustion and Flame 159.11 (2012), pp. 3398–3413.
- [17] Pierre Wolf, Gabriel Staffelbach, Laurent Y.M. Gicquel, Jens-Dominik Müller, Thierry Poinot. Acoustic and Large Eddy Simulation studies of azimuthal modes in annular combustion chambers. Combustion and Flame, Elsevier, 2012, vol. 159,

pp. 3398-3413. 10.1016/J.combustion and flame, 2012.06.016.hal-00801825

- [18] Chase, M.W., NIST-JANAF Thermochemical Tables, Fourth Edition, Monograph 9 (Part I and Part II), pp. 1963, 1998.
- [19] Spalding, D.B., Mixing and chemical reaction in steady confined turbulent flames., In: Thirteenth Symposium (International) on Combustion, pp. 649–657, The Combustion Institute, Pittsburgh, PA, 1970.
- [20] Cant, R.S. and Bray, K.N.C., Strained Laminar Flamelet Calculations of Premixed Turbulent Combustion in a Closed Vessel, In Twenty-Second Symposium (International) on Combustion, pp. 791-799, The Combustion Institute, 1990.
- [21] Masuya, G., Influence of Laminar Flame Speed on Turbulent Premixed Combustion, Combustion and Flame, 64, pp. 353-367, 1986.
- [22] Weller, H. G., Tabor, G., Gosman, A. D., Fureby, C., Application of a Flame-Wrinkling LES Combustion Model to a Turbulent Mixing Layer Twenty-Seventh Symposium (International) on Combustion/The Combustion Institute, pp. 899–907, 1998.
- [23] Tabor, G. and Weller, H.G., Large Eddy Simulation of Premixed Turbulent Combustion Using Flame Surface Wrinkling Model, Turbulence and Combustion 72: pp. 1–28, 2004.
- [24] Colin, O., Ducros, F., Veynante, D. and Poinso, T., A thickened flame model for large eddy simulations of turbulent premixed combustion. Phys. Fluids 12(7), pp. 1843–1863, 2000.
- [25] Pope, S.B., The Evolution of Surfaces in Turbulence, International Journal of Engineering Science, 26(5), pp. 445-469, 1988.
- [26] Cant, R.S., Pope, S.B. and Bray, K.N.C., Modelling of Flamelet Surface-to-Volume Ratio in Turbulent Premixed Combustion, In Twenty-Third Symposium (International) on Combustion, pp. 809-815, The Combustion Institute, 1990.
- [27] Weller, H.G., Marooney, C.J. and Gosman, A.D., A New Spectral Method for Calculation of the Time-Varying Area of a Laminar Flame in Homogeneous Turbulence, In Twenty-Third Symposium (International) on Combustion, pp. 629-636, The Combustion Institute, 1990.
- [28] Weller, H.G., Usla, S., Gosman, A.D., Maly, R.R., Herweg, R. and Heel, B., Prediction of Combustion in Homogeneous-Charge Spark-Ignition Engines, In Twenty-Second Symposium COMODIA 94, pp. 163-169, The Japan Society of Mechanical Engineers, 1994.
- [29] Weller, H.G., The development of a new flame area combustion model using conditional averaging. Thermo-fluids section report TF 9307, Department of Mechanical Engineering, Imperial College of Science, Technology and Medicine, 1993.
- [30] Gülder, Ö.L., Turbulent premixed flame propagation models for different combustion regimes, In Twenty-Third Symposium (International) on Combustion, Volume 23(1), pp. 743-750, The Combustion Institute, 1991.
- [31] Weller, H.G., Tabor, G., Jasak, H., and Fureby, C.: A tensorial approach to computational continuum mechanics using object orientated techniques, Computers in Physics, 12(6):620 – 631, 1998.
- [32] Christopher J. Greenshields, OpenFOAM: The Open Source CFD Toolbox Programmer's Guide, Version 3.0.1, OpenFOAM Foundation Ltd, December 2015.
- [33] Jasak, H. and Gosman, A.D.: Automatic resolution control for the Finite Volume Method. Part 1: A-posteriori error estimates, Numerical Heat Transfer, Part B, 38(3):237–256, September 2000.
- [34] Jasak, H. and Gosman, A.D.: Residual error estimate for the Finite Volume Method, Int. Journal of Numerical Methods and Fluids, 39:1–19, 2001.
- [35] Hirt, C. W., Amsden, A. A., Cook, J. L., An Arbitrary Lagrangian–Eulerian Computing Method for All Flow Speeds, Journal of Computational Physics 135, pp. 203–216, Article No. CP975702, 1997.
- [36] Anthony A. A., KIVA-3V: A Block-Structured KIVA Program for Engines with Vertical or Canted Valves, Los Alamos National Laboratory, Los Alamos, New Mexico 87545, LA-13313-MS, UC-1412, July 1997.
- [37] Lancaster, D.R., Kreiger, R.B., Sorenson, S.C. and Hull, W., Effects of Turbulence on Spark-ignition Engine Combustion, Society of Automotive Engineers, 760160, Detroit, 1976.

ИСТРАЖИВАЊЕ СИМУЛАЦИЈЕ САГОРЕВАЊА КОД БЕНЗИНСКОГ МОТОРА КОРИШЋЕЊЕМ СОФТВЕРА OPENFOAM

Л. Анетор, Е.Е. Осакуе, К. Харис

Софтвер отвореног кода OpenFOAM је коришћен за проучавање перформанси модерног 4-вентилског, изооктанског мотора, са потпуним мешањем, са две брегасте осовине изнад главе мотора, са квази симетричном двостраном кровном комором за сагоревање, при брзини од 1500 обртаја по секунди. Највиши притисак се развио у горњој мртвој тачки и имао вредност приближно 30 бара. Резултати показују да се максимална температура сагоревања јавља када је угао осовине после горње мртве тачке приближно 90° , запреминска просечна температура је приближно 2700°K , али је утврђено да је стварни пик температуре 3000°K и настаје у положају 12630 тачке решетке. Вредности температуре веће од запреминске просечне температуре кретале су се од $2968,81^{\circ}\text{K}$ до $2974,01^{\circ}\text{K}$ што одговара положајима тачака решетке од 12630 до 12633. Утврђено је да се фактор набороног фронта пламена креће у распону $1,0 \leq \Xi \leq 3,8$. Динамика регресије променљиве била је тачно предвиђена.