Engine Block Vibrations – An Indicator of Knocking in the SI Engine

The factors influencing the onset of knocking have a significant impact on how well a SI engine performs. Hence, the efficacy in determining the onset and controlling of knock is a key factor in improving the SI engine’s performance. This paper provides insight into the role of engine block vibrations in determining the occurrence of knock using Empirical Mode Decomposition and Short-Time Fourier Transform. To comprehend the behaviour of vibration amid normal combustion and knocking conditions, the engine block vibration signals are analyzed and compared with the in-cylinder pressure fluctuations. The features of knock are extracted from the engine block vibration signals using Empirical Mode Decomposition. The first Intrinsic Mode Function (IMF) thus obtained is used to generate the Hilbert spectrum for detecting the occurrence of knock. Similarly, Short-Time Fourier Transform is also performed on the first IMF to obtain the spectrogram. The findings demonstrate unequivocally that higher frequency variations are produced when knock occurs. These results also indicate that the combination of Empirical Mode Decomposition and Short-Time Fourier Transform can be used effectively for determining the occurrence of knock.

Keywords: Spark Ignition Engine, Knocking, Empirical Mode Decomposition, Hilbert Transform, Short-time Fourier Transform, Spectrogram.

1. INTRODUCTION

The stringent emission norms and the issues pertaining to climatic changes had made the researchers consider alternate fuels or improving the performance of conventional fueled engines. The studies show that the performance of the SI engines improves with the compression ratio; however, it results in knocking above a particular value, called Highest Useful Compression Ratio (HUCR) [1]. Hence, the improvement in the performance of SI engines will not be possible beyond a certain limit. However, the knock could be suppressed to a certain extent by reducing the in-cylinder temperature [1]. Cooled Exhaust Gas Recirculation, water injection system, emulsified fuel, etc., could be used to extend the HUCR. Further improvement in the performance could be possible only if there is a possibility of real-time monitoring and control of SI engine knocking. Real-time SI engine knock suppression may be accomplished with cooled EGR [2]. However, the effectiveness in controlling the SI engine knock and improvement in the performance of an engine depends on how accurately we can predict the occurrence of knock. Many studies are available for predicting the occurrence of knock; based on the fuel octane number, ignition timing, in-cylinder pressure, temperature, the air-fuel ratio, etc. [3-6]. Due to the complexity, these studies failed to be efficiently employed for the real-time detection of knock. This leads to the study of the behavior of various parameters that may be affected during the occurrence of a knock. Nano-fluids were utilized as the coolant by Ollivier et al. [7] to explore the transient temperature fluctuations that occurred during the onset of knock. To amplify the transient temperature fluctuations, grooves facing the coolant flow were added to the cylinder liner [7]. This method could effectively detect the occurrence of knock. However, the time lag caused during the occurrence of temperature fluctuations and its analysis to confirm the knock makes it unfit for real-time monitoring and control of knock.

In-cylinder pressure, acoustic signals, and engine block vibrations are used by many researchers for the detection and analysis of knock [2, 8, 9]. The acoustic signals captured from the engine consist of noise, which requires proper analysis before extracting the features of knock. There are many methods for denoising the signals; among them, wavelets are found to be effective [8, 10, 11]. Also, there are various mathematical tools for analyzing denoised signals, including the Fourier transform, Wavelet transform, Empirical Mode Decomposition (EMD), etc. [12-18]. Furthermore, there are many variations and extensions of these models for extracting the features from the signals more efficiently and accurately [2, 9, 19, 20, 21]. Standard Fourier and Wavelet approaches use predefined functions as the basis for analyzing the signals [13, 22]. The Fourier analysis could be done only if there is at least one full wave oscillation of a sine or cosine wave to obtain the local frequency [13]. Therefore, the instantaneous frequency cannot be calculated for non-stationary data that changes the frequency now and then. Wavelet analysis could provide physically meaningful interpretations more accurately to only linear signals...
the occurrence of knock as well as to classify the knock based on its intensity. However, the engine block vibration analysis finds application in (i) detecting the malfunctioning of the moving parts, (ii) determining the engine performance, and (iii) designing the other parts of the vehicles [28-30]. The location at which the vibration signals are captured, as well as the methods adopted for analyzing the signals, are different for each purpose. Hence, research is going on to identify the most accurate and simple methods for each purpose.

In this work, the in-cylinder pressure and denoised vibration signals are analyzed to extract the features of knock. The signals are decomposed using EMD, even though there are many improved models like EEMD [9, 20], Complementary Ensemble Empirical Mode Decomposition [31], etc. This is due to the better adaptability of EMD in decomposing the signals, i.e., it could naturally deal with the non-stationarities and non-linearities. Thus, it could be used effectively in extracting the features of the knock from the signals in real-time situations. Current work focuses on various methods that could be adopted for extracting the features of knock within the limitations of EMD and to develop a criterion for detecting the SI engine knock that could lead towards knock detection and control its further occurrence in real-time. The Hilbert Spectrum of the first IMF obtained using EMD is analyzed to study the features of knock. The spectrum is also obtained by performing Short-Time Fourier Transform (STFT) on the first IMF obtained using EMD. The results are compared to choose the optimal strategy, which could determine the occurrence of knock effectively. The following sections address the details regarding the methodologies used and the results obtained.

2. ENGINE BLOCK VIBRATION ANALYSIS AND SYSTEM CONTROL

In-cylinder pressure and the corresponding engine block vibration signals are taken from the research by Fengrong et al. [31-33]. They had captured the signals from 4 cylinders, 4-stroke, in-line SI engine. The ignition timing is advanced to induce knock. Two DYTRAN - 621B40 [31-33] accelerometers were mounted on the engine block (nearby cylinders 2 and 4) to capture the vibrations with a sampling frequency of 51,200 Hz. The pressure transducer AVL - GH13Z-31(24) was used to measure in-cylinder pressure signals [31-33]. From the literature, it is noted that the signals generated during knock contain frequencies ranging from 8 kHz to 22 kHz [9]. For better accuracy, the noise needs to be eliminated before analyzing the signals. Denoising is achieved by applying signal filtering techniques using wavelet filters. The use of soft thresholding minimizes the chance of discontinuities in the denoised signal [34]. The Symlet wavelet is used for denoising the signal since it could reduce the phase distortion due to its better symmetry. The denoised signal is then decomposed using EMD to extract the features of knock. The first intrinsic mode function (IMF1) thus acquired bears the characteristics of knock. Hence, in the current work, only the first IMF is used to study the behavior of knock, even though other IMFs also might contain the features of knock due to the
mode mixing that may arise with the use of EMD. This will also help to ensure a simple methodology to timely address the occurrence of a knock with less computation. Hilbert spectrum and spectrogram of IMF1 are obtained to compare its effectiveness in determining the occurrence of knock. The following sections contain additional details about the analysis.

2.1 EMD Algorithm

EMD was developed by N Huang [13] for analyzing non-stationary signals. A signal could be broken down using EMD into various components with gradually changing amplitude and phase [18]. This property enables it to obtain intrinsic patterns at multiple scales without assuming that the signal is harmonic in nature, stationary, etc., as we do in wavelet Transform or Fourier analysis [22]. The iterative process followed in EMD for obtaining the IMFs, called sifting, and the algorithm used for it is as follows [22]:

- Find the locations of all the extrema in the signal (local extrema), \(x(t)\).
- Obtain the lower envelope, \(e_{\text{lower}}(t)\), by interpolating between all the local minima. Similarly, obtain the upper envelope, \(e_{\text{upper}}(t)\), by interpolating between all the local maxima.
- Compute the local mean, \(m(t)\), from local minima, \(e_{\text{lower}}(t)\), and local maxima, \(e_{\text{upper}}(t)\), obtained.
- Subtract ‘local mean’ from ‘local extrema’ to obtain the ‘modulated oscillation’, \(d(t) = x(t) - m(t)\).
- If the modulated oscillation obtained satisfies the stopping criterion, then it is taken as the first IMF, \(IMF_1 = d(t)\), so that the new local extrema becomes \(x(t) = x(t) - IMF_1\), else set it as the new local extrema \(x(t) = d(t)\) and start reiterating from step 1.

This process is repeated until all the IMFs are obtained, and the residue becomes a monotonic function. The stopping criterion checks whether the modulated oscillation satisfies the properties of the IMF, which is as follows [13]:

- Either the extrema and the number of zero crossings must be equal, or they can only differ by one.
- The Mean value of the lower/upper envelope at any point should be zero.

Thus, after the sifting process, IMFs are obtained from which instantaneous frequency can be defined. By using EMD, we can have inter-wave frequency modulations to explain the waveform deformation due to non-linear effects and intra-wave frequency modulation to explain the dispersive propagation of waves [13]. Also, the signal that is decomposed using EMD can be reconstructed perfectly [22]. Amidst all these positives, mode mixing and aliasing are its drawbacks. Mode mixing occurs when either one oscillatory mode is present in multiple IMFs or more than one oscillatory mode is present in one IMF [22]. Aliasing is the overlapping of IMF spectra formed due to the sub-Nyquist nature of extrema sampling [20].

2.2 Hilbert Spectrum

The Hilbert Transform offers a special approach to defining the imaginary components, though there are multiple theoretical ways to do so. The results, thus, obtained will be an analytic function [13]. A signal can be simultaneously represented in the time and frequency domains by using Hilbert Spectrum [18]. This spectrum works well for pinpointing the locations in time and frequency space where the majority of the energy is concentrated. Hence, it can be used as an important tool in determining the occurrence of a knock and the cylinder at which the knock is occurring. As energy will be focused in the high-frequency regions during the knock occurrence, the resulting Hilbert Spectrum will give an intuitive vision of how much energy is localized in the high-frequency range and when it is occurring. Hence, it would be a great choice for non-stationary and non-linear data analysis. However, the simple Hilbert Transform of the denoised vibration signals contains the entire details about the frequency content of a signal, as it may contain more than one oscillatory mode at any instant [35]. Therefore, rather than finding the Hilbert Transform of a complete signal, it is applied to the first IMF obtained after performing EMD. As a result, using the Hilbert Spectrum, we could derive the localized data associated with the signal in the frequency domain. This, in turn, could identify the hidden local data structures that are embedded in the original signal [14]. In the current work, the Hilbert Spectrum of the first IMF obtained using EMD is plotted to study its effectiveness in determining the occurrence of knock.

2.3 Short-Time Fourier Transform

In contrast to the Fourier Transform, Short-time Fourier Transform (STFT) could provide time-localized information about a signal whose frequency varies with time, while the former could only provide time-averaged information about the frequency [36]. Hence, STFT finds application in analyzing non-stationary signals. Moreover, it requires lower computational power. The vibration signal was mapped into a 2-D function of time and frequency by Al-Badour et al. [37] using STFT. In STFT, a non-stationary signal is separated into discrete time frames of identical length before being processed using Fourier transform [38]. Hence, any changes occurring in the signal at any instant could be captured in a time frame. However, EMD is more powerful in capturing all the physics of non-stationary non-linear signals than STFT. Therefore, in the current work, we used a combination of EMD and STFT to utilize the advantages of both. STFT is applied on the first IMF that is obtained after performing EMD of the vibration signal to establish the spectrogram. Thus, the advantage of EMD in extracting the features of the knock from the vibration signal can be utilized. At the same time, we will get a meaningful representation of the knock signal in a spectrogram, which is an intensity plot of STFT magnitude over time.

2.4 Knock detection using In-cylinder pressure

To quantify the intensity of knock, the maximum amplitude of pressure oscillation (MAPO) method was used. If the MAPO surges above 0.5 bar, the correlates—ponding cycle is treated as a knocking cycle. While if it is even
higher than 2 bar, it is treated as a strong knock [39]. MAPO is obtained using the following relation [39].

\[
\text{MAPO} = \max \left( \hat{P}_{\theta_0 + \delta} \right)
\]

Here \( \hat{P} \) is the filtered pressure that was obtained after passing the in-cylinder pressure through a band-pass filter between the frequencies 6 – 20 kHz. \( \theta_0 \) is the crank angle corresponding to the initiation of combustion and \( \delta \) is the duration of combustion.

The effectiveness of representing the knock signals using the Hilbert Spectrum and spectrogram is addressed in the current work and is explained in the following section. Also, the Hilbert Spectrum and spectrogram are compared along with the MAPO to study their effectiveness in classifying the knock based on its intensity.

3. RESULTS AND DISCUSSION

Figures 1 and 2 show the in-cylinder pressure fluctuations with and without the occurrence of knock [31-33]. EMD was used to decompose the engine block vibration signals that corresponded to the in-cylinder pressure signals shown in Figs. 1 and 2 [31-33]. Figures 3 and 4 show the IMFs obtained on decomposing the vibration signals produced during the presence and absence of knock, respectively. From Fig. 3 and 4, it is clear that vibrations up to 100 g are produced during the SI engine knock, while the maximum amplitude is only 20 g during the absence of knock. Higher amplitudes in the IMF 1 obtained may be concluded as due to the occurrence of knock. The presence of knock could not be determined just by the fluctuation in the amplitudes of the vibration signals, as was the case with the variations in the in-cylinder pressure. There may be other factors also that cause amplitude fluctuations in the engine block vibrations. Therefore, for further analysis and confirmation, we performed investigations using the Hilbert Spectrum and spectrogram to visualize the energy distribution of the signal at various frequency levels.

![Figure 1: In-cylinder pressure during the occurrence of knock [33].](image)

![Figure 2: In-cylinder pressure during the absence of knock [33].](image)

![Figure 3: First five IMFs obtained after decomposing the engine block vibration signals using EMD. The signal was captured during the presence of a knock.](image)

![Figure 4: First five IMFs obtained after decomposing the engine block vibration signals using EMD. The signal was captured during the non-knocking cycle.](image)

![Figure 5: Hilbert Spectrum of the first IMF obtained after performing EMD on the engine block vibration signals produced during the absence of knock.](image)
MAPO is calculated to be 5.46 bar and 0.237 bar corresponding to the in-cylinder pressures shown in Fig. 1 and 2, indicating the presence of a very strong knock and the absence of knock, respectively.

Figures 5 – 8 show the Hilbert spectrum and spectrogram corresponding to the IMF1 obtained during the occurrence of knock and non-knock conditions. From Fig. 6, it is observed that the energy level of the vibration signal falls in the higher frequency ranges, above 20 kHz, during the occurrence of knock. While this was not visible in the Hilbert Spectrum obtained for the normal combustion process (Fig. 5). However, studies revealed that the vibrations are generated when a knock occurs in a range of frequencies between 8 to 22 kHz [9]. From Fig. 5, we can see that the energies of vibration fall in frequencies above 10 kHz even during the normal combustion process. Therefore, it might be difficult to compare the signals for determining the occurrence of knock during the continuous working of an SI engine. To strengthen this, additional analysis of the signals containing data on engine block vibrations generated during combustion in all cylinders in an engine is required.

Alike the Hilbert spectrum, STFT of the IMF 1 was done to obtain the spectrogram, as shown in Fig. 7 and 8. The findings demonstrate that, in contrast, to the normal combustion process, the energy level of the signal is high when a knock occurs. Also, we could see that there are higher energy levels in the frequency range above 20 kHz during the occurrence of knock (Fig. 8). However, we can see that some lower energy level also falls in the high-frequency range during the normal combustion process (in the absence of knock) (Fig. 7). This is not visible in the Hilbert Spectrum of the vibration signals produced during non-knocking cycles. Similar to that of the Hilbert Spectrum, a spectrogram could also be used to identify the time as well as the cylinder in which the knock is occurring. Further investigations are required to find the effectiveness of the Hilbert Spectrum and spectrogram for determining the occurrence of knock, especially when the signal that is to be analyzed is captured from a multi-cylinder engine. This is because the effectiveness of the results may depend on the sample length of the signal and engine operating parameters like engine speed, the torque developed, etc. Also, the spectrogram or Hilbert Spectrum may change if the sample signal consists of a combination of vibrations produced during the presence and absence of knock.
Figure 9: In-cylinder pressure [33] and first five IMFs obtained after decomposing the engine block vibration signals captured at 2800 rpm using EMD.

Figure 10: In-cylinder pressure [33] and first five IMFs obtained after decomposing the engine block vibration signals captured at 4000 rpm using EMD.

Figure 11: Hilbert spectrum of the IMF 1 obtained after performing EMD on the engine block vibration signals captured at 2800 rpm.

Figure 12: Hilbert spectrum of the IMF 1 obtained after performing EMD on the engine block vibration signals captured at 4000 rpm.

Figure 11 and 12 shows the Hilbert spectrum corresponding to the first IMFs obtained after decomposing the engine block vibration signals shown in Fig. 9 and 10, respectively. In the Hilbert Spectrum obtained, the energy distribution is found to have frequencies above 8 kHz corresponding to the combustion process in each cylinder. Furthermore, the intensity of energy in the higher frequency range is found to be high, around 0.005 seconds and 0.0165 seconds (Fig. 11) and 0.011 seconds and 0.026 seconds (Fig. 12), respectively, for both cases. On comparing the amplitude of the vibrations and their corresponding energy distribution in the Hilbert Spectrum, we could infer that the higher amplitude vibrations corresponding to 5 ms and 16.5 ms shown in Fig. 9 are due to the occurrence of knock. This is due to the higher energy vibration signals with higher frequencies produced during these instances. However, this was absent in the higher amplitude vibrations around 37.5 ms; hence it may not be due to the occurrence of knock.

Figure 13 and 14 shows the spectrogram of the first IMFs of the signals given in Fig. 9 and 10. From Fig. 13, it is clear that the vibration energy is maximum at 0.004721 seconds. Also, there are energy levels in the higher frequency regions (above 15 kHz) during the same period. Hence, it could be concluded as a strong knock. The MAPO is corresponding to this in-cylinder
The methodology described in this work could be used to detect the presence of knock with minimum computation. Emphasis was given to identifying a mechanism to determine the knocking cycles so that it could be used in real-time. However, all the features of knock could not be extracted using EMD due to the mode mixing. The findings, however, demonstrate that the vibration signals captured from the engine block alone could be used to extract the features of knock. This reduces the cost incurred for the sensors and the computational power for using in-cylinder pressure to determine the knock. According to the observations from the current work, the criterion for detecting the presence of knock may be fixed as the first IMF that exceeds the amplitude of 20g and has frequencies above 10 kHz taken together. Furthermore, the energy intensity of vibration signals falling in the higher frequency range above 10 kHz can be analyzed to categorize the knock as strong or weak.

The engine block vibration signals are decomposed using EMD. The first IMF obtained after decomposing the vibration signals produced while knock occurs evaluated with that obtained during the non-knocking cycle. The higher amplitude fluctuations in the signal could be used to locate the occurrence of knock in the time domain. However, this alone is not sufficient to confirm the occurrence of knock. Hilbert spectrum and spectrogram of the signal are obtained to demonstrate the amplitude fluctuations of the signal in a time-frequency domain. The results show that, during the occurrence of knock, the amplitude of signals falls in the high-frequency region, i.e., above 10 kHz. From the Hilbert spectrum and the spectrogram of the signal, it is clear that both could be used individually to determine the occurrence of knock and also to locate the cylinder at which it is occurring. Further studies reveal that the combination of EMD and STFT (spectrogram) provides more clarity than the Hilbert spectrum obtained after EMD alone. MAPO calculated using the in-cylinder pressures also produced the same inferences as that obtained using the Spectrogram. The current study also shows that the vibration signals captured from the engine block alone could be used to extract the features of knock. This reduces the cost incurred for the sensors and the computational power for using in-cylinder pressure to determine the knock. According to the observations from the current work, the criterion for detecting the presence of knock may be fixed as the first IMF that exceeds the amplitude of 20g and has frequencies above 10 kHz taken together. Furthermore, the energy intensity of vibration signals falling in the higher frequency range above 10 kHz can be analyzed to categorize the knock as strong or weak.

From Figures 11 - 14, it is evident that the maximum value of energy at the higher frequency region is not constant. Hence, proper experiments need to be conducted to find the energy level of the vibrations produced during the knocking cycles that occur in the entire engine operating range for fixing the threshold values. Information regarding the firing order and the engine speed are the only additional data required for identifying the cylinder in which knock is produced. We can also see that in both the Hilbert Spectrum and the spectrogram obtained, energy distribution of the vibration signals is also observed above 10 kHz for both the knock and non-knock conditions. However, the maximum value of energy at the higher frequency region is the knock and non-knock conditions. However, the vibration signals is also observed above 10 kHz for both spectrogram obtained, energy distribution of the cylinder in which knock is produced. We can also see that in both the Hilbert Spectrum and the spectrogram obtained, energy distribution of the vibration signals is also observed above 10 kHz for both the knock and non-knock conditions. However, the

Figure 13: Spectrogram plotted using the IMF 1 obtained after performing EMD on the engine block vibration signals captured at 2800 rpm.

Figure 14: Spectrogram plotted using the IMF 1 obtained after performing EMD on the engine block vibration signals captured at 4000 rpm.

4. CONCLUSION

The engine block vibration signals are decomposed using EMD. The first IMF obtained after decomposing the vibration signals produced while knock occurs evaluated with that obtained during the non-knocking cycle. The higher amplitude fluctuations in the signal could be used to locate the occurrence of knock in the time domain. However, this alone is not sufficient to confirm the occurrence of knock. Hilbert spectrum and spectrogram of the signal are obtained to demonstrate the amplitude fluctuations of the signal in a time-frequency domain. The results show that, during the occurrence of knock, the amplitude of signals falls in the high-frequency region, i.e., above 10 kHz. From the Hilbert spectrum and the spectrogram of the signal, it is clear that both could be used individually to determine the occurrence of knock and also to locate the cylinder at which it is occurring. Further studies reveal that the combination of EMD and STFT (spectrogram) provides more clarity than the Hilbert spectrum obtained after EMD alone. MAPO calculated using the in-cylinder pressures also produced the same inferences as that obtained using the Spectrogram. The current study also shows that the vibration signals captured from the engine block alone could be used to extract the features of knock. This reduces the cost incurred for the sensors and the computational power for using in-cylinder pressure to determine the knock. According to the observations from the current work, the criterion for detecting the presence of knock may be fixed as the first IMF that exceeds the amplitude of 20g and has frequencies above 10 kHz taken together. Furthermore, the energy intensity of vibration signals falling in the higher frequency range above 10 kHz can be analyzed to categorize the knock as strong or weak.

The methodology described in this work could be used to detect the presence of knock with minimum computation. Emphasis was given to identifying a mechanism to determine the knocking cycles so that it could be used in real-time. However, all the features of knock could not be extracted using EMD due to the mode mixing. The findings, however, demonstrate that
spectrograms may accurately capture the vibration signals generated during SI engine knock in their time-frequency domain, even if some characteristics may have been lost while decomposing.

The pattern of the spectrograms obtained for the several knocking and non-knocking cycles could be used to train the machine learning algorithm. Thus the current work can be extended further to determine the knocking cycles and to take appropriate control measures, such as the reduction in the in-cylinder temperatures using cooled Exhaust Gas Recirculation, etc., to prevent its further occurrence of knock in real-time.

REFERENCES
NOMENCLATURE
\( \hat{P} \) Filtered pressure having frequencies between 6-20 kHz is the
\( x'(t) \) Local extrema
\( e_{\text{mid}}(t) \) Lower envelope
\( e_{\text{up}}(t) \) Upper envelope
\( d(t) \) Modulated oscillation

Greek symbols
\( \theta_0 \) Ignition timing
\( \delta \) Duration of combustion

ACRONYMS AND ABBREVIATIONS
HUCR Highest Usable Compression Ratio
EMD Empirical Mode Decomposition
IMFs Intrinsic Mode Functions
EEMD Ensemble Empirical Mode Decomposition
STFT Short-Time Fourier Transform
MAPO Maximum Amplitude of Pressure Oscillation
BTDC Before Top Dead Centre

ВИБРАЦИЈЕ БЛОКА МОТОРА - ИНДИКАТОР КУЦАЊА У СИ МОТОРУ

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Фактори који утичу на почетак куцања имају значајан утицај на то колико добро СИ мотор ради. Дакле, ефикасност у одређивању почетка и контроли детонације је кључни фактор у побољшању перформанси СИ мотора. Овај рад јаје увид у улогу вибрација блока мотора у одређивању појаве детонације коришћењем емпиријског декомпозиције и краткорочне Фурјеове трансформације. Да би се разумело понашање вибрација у условима нормалног сагоревања и куцања, сигнали вибрације блока мотора се анализирају и упоређују са флуктуацијама притиска у цилинду. Качерастичност куцања се изражава из вибрацијских сигнала блока мотора коришћењем емпиријског режима декомпозиције. Права тако добијена функција унутрашњег мода (ИМФ) се користи за генерисање Хилбертовог спектра за откривање појаве детонације. Слично, краткорочна Фурјеова трансформација се такође изводи на првом ИМФ-у за добијање спектрограма. Налази недвосмислено показују да се већи варијацији фрактакење произведе када дође до куцања. Ови резултати такође указују на то да се комбинација емпиријског модуса декомпозиције и краткорочна Фурјеова трансформације може ефикасно користити за одређивање појаве детонације.